

# Physics and Applications of Spin-Transfer Torques

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**CQP** Center for  
Quantum  
Phenomena

# Physics and Applications of Spin-Transfer Torques

## Outline

- Magnetic tunnel junctions and spin-transfer torques
- Applications
- Switching of magnetization, materials and device optimization
- Cryogenic applications



# Giant Magnetoresistance (GMR)



The Nobel Prize in Physics 2007

"for the discovery of Giant Magnetoresistance"



**Albert Fert**

**Peter Grünberg**

1/2 of the prize

1/2 of the prize

France

Germany

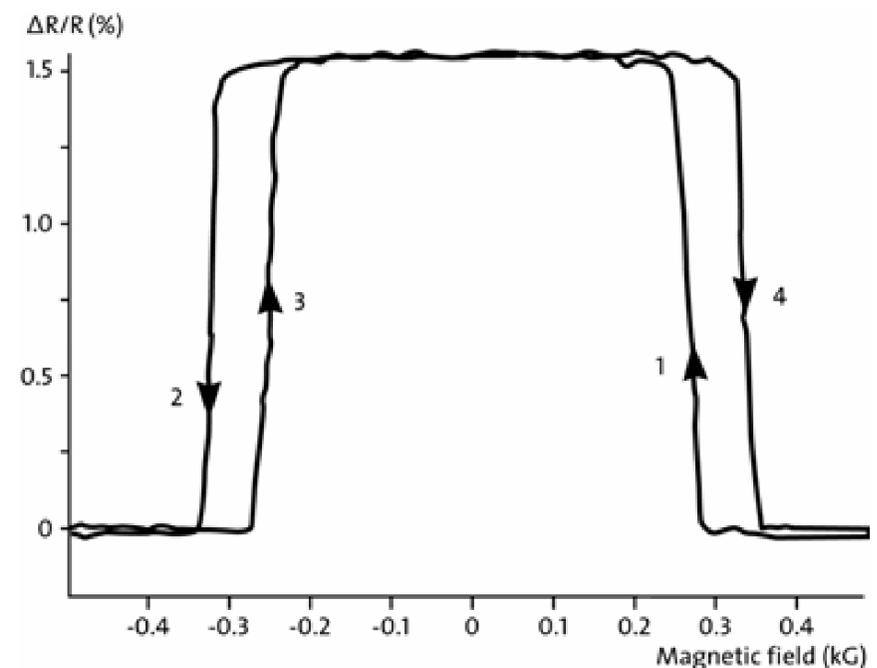
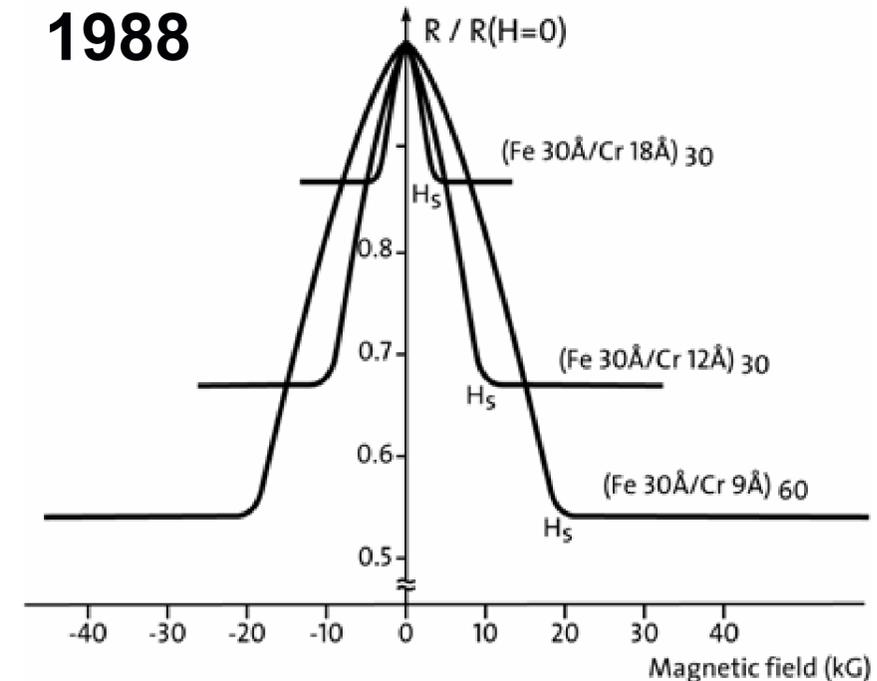
Université Paris-Sud;  
Unité Mixte de Physique  
CNRS/THALES  
Orsay, France

Forschungszentrum Jülich  
Jülich, Germany

b. 1938

b. 1939

1988



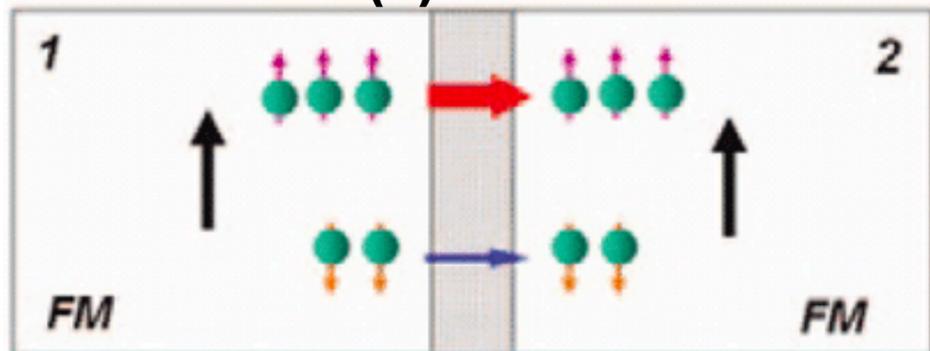
→ **'Spintronics' = Spin+Transport+Electronics: control of current using the spin of electrons**



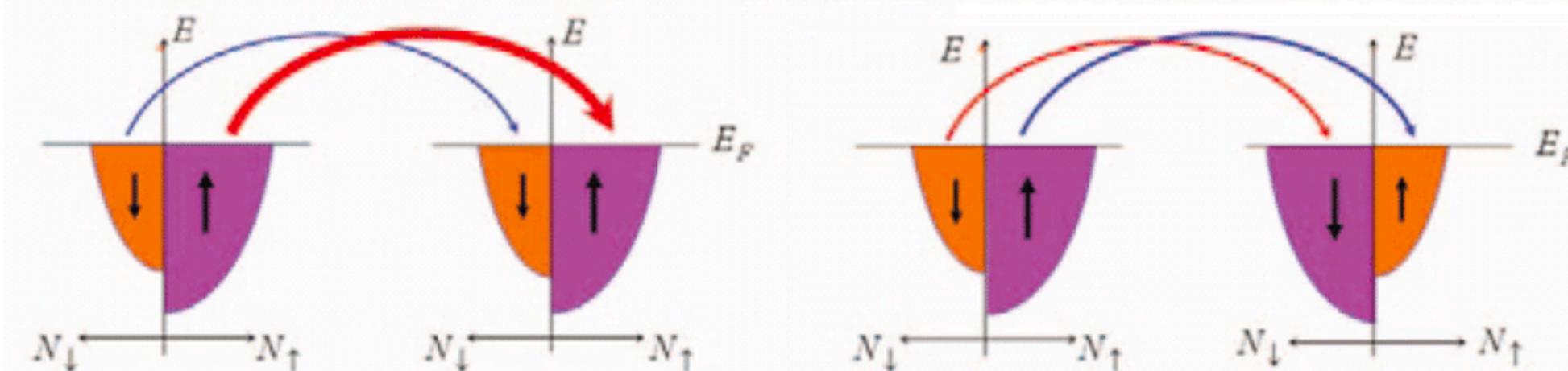
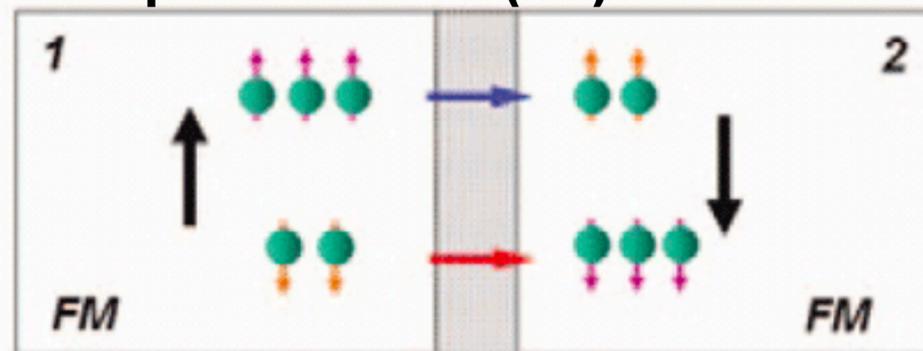
# Magnetic Tunnel Junction

Two ferromagnetic metals separated by an insulating barrier

Parallel state (P)



Anti-parallel state (AP)

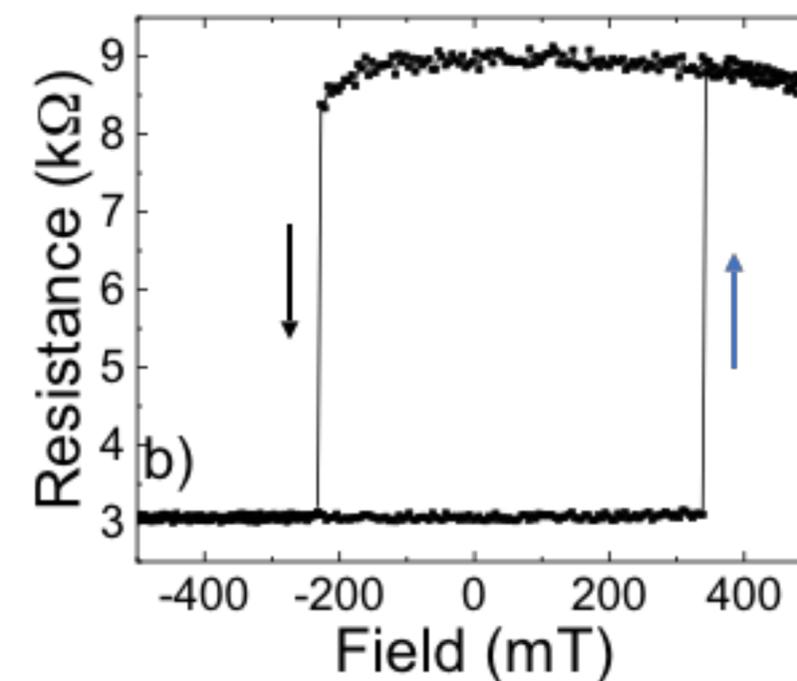
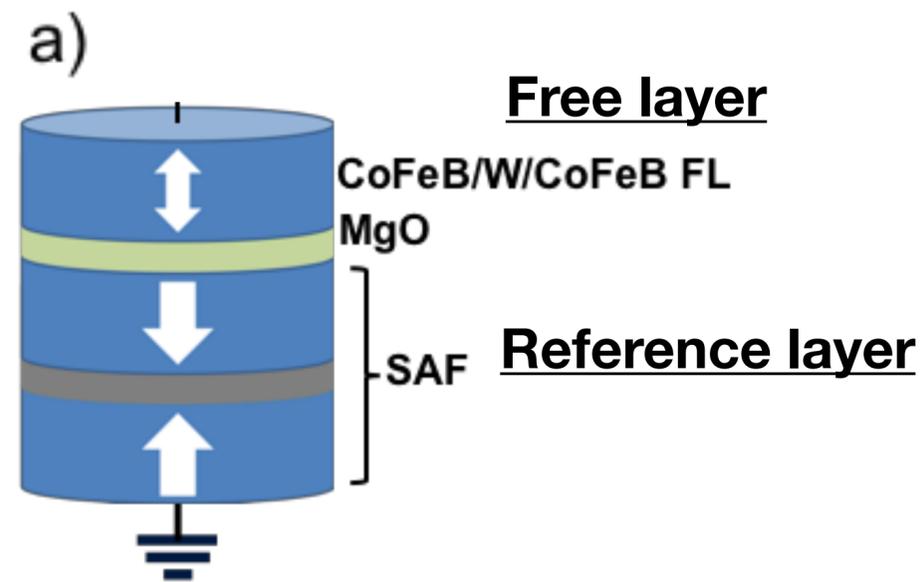


From:

$$P_i = \frac{N_{i\uparrow}(E_F) - N_{i\downarrow}(E_F)}{N_{i\uparrow}(E_F) + N_{i\downarrow}(E_F)}$$

Julliere's formula: 
$$\text{TMR} = \frac{R_{AP} - R_P}{R_P} = \frac{2P_1P_2}{1 - P_1P_2}$$

W. H. Butler *et al.*, Spin-dependent tunneling conductance of Fe|MgO|Fe sandwiches  
PRB **63**, 054416 (2001)





# Prediction of Spin-Transfer Torques

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2013 Oliver E. Buckley Prize

**John Slonczewski**

**Luc Berger**

**Citation:**

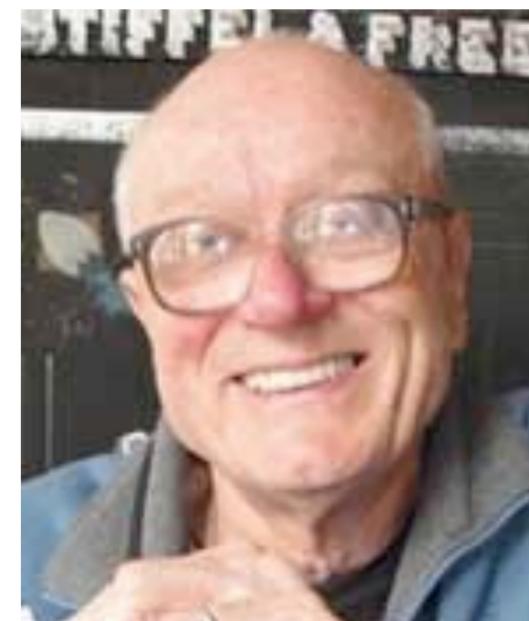
“For predicting spin-transfer torque and opening the field of current-induced control over magnetic nanostructures.”

**Foundational papers:**

J. C. Slonczewski, Phys. Rev. B. **39**, 6996 (1989)

J. C. Slonczewski, J. Magn. Mater. **159**, L1 (1996)

L. Berger, Phys. Rev. B **54**, 9353 (1996)





# Prediction of Spin-Transfer Torques

PHYSICAL REVIEW B

VOLUME 39, NUMBER 10

1 APRIL 1989

## Conductance and exchange coupling of two ferromagnets separated by a tunneling barrier

J. C. Slonczewski

IBM Research Division, Thomas J. Watson Research Center, Yorktown Heights, New York 10598

(Received 27 June 1988)

A theory is given for three closely related effects involving a nonmagnetic electron-tunneling barrier separating two ferromagnetic conductors. The first is Julliere's magnetic valve effect, in which the tunnel conductance depends on the angle  $\theta$  between the moments of the two ferromagnets. One finds that discontinuous change of the potential at the electrode-barrier interface diminishes the spin-polarization factor governing this effect and is capable of changing its sign. The second is an effective interfacial exchange coupling  $-J \cos\theta$  between the ferromagnets. One finds that the magnitude and sign of  $J$  depend on the height of the barrier and the Stoner splitting in the ferromagnets. The third is a new, irreversible exchange term in the coupled dynamics of the ferromagnets. For one sign of external voltage  $V$ , this term describes relaxation of the Landau-Lifshitz type. For the opposite sign of  $V$ , it describes a pumping action which can cause spontaneous growth of magnetic oscillations. All of these effects were investigated consistently by analyzing the transmission of charge and spin currents flowing through a rectangular barrier separating free-electron metals. In application to Fe-C-Fe junctions, the theory predicts that the valve effect is weak and that the coupling is antiferromagnetic ( $J < 0$ ). Relations connecting the three effects suggest experiments involving small spatial dimensions.

$$\text{TMR} = \frac{2P_1 P_2}{1 - P_1 P_2}$$

### In magnetic tunnel junctions

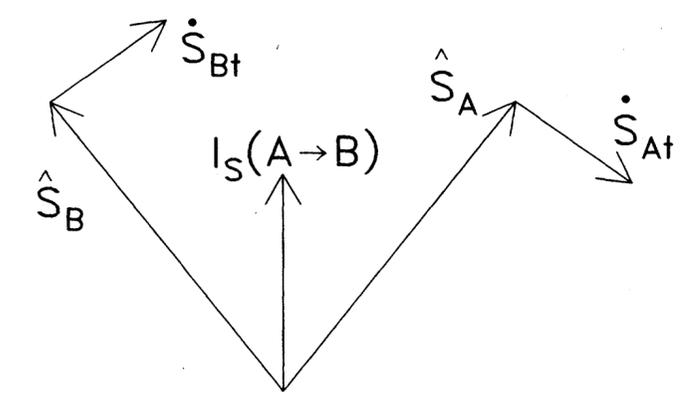
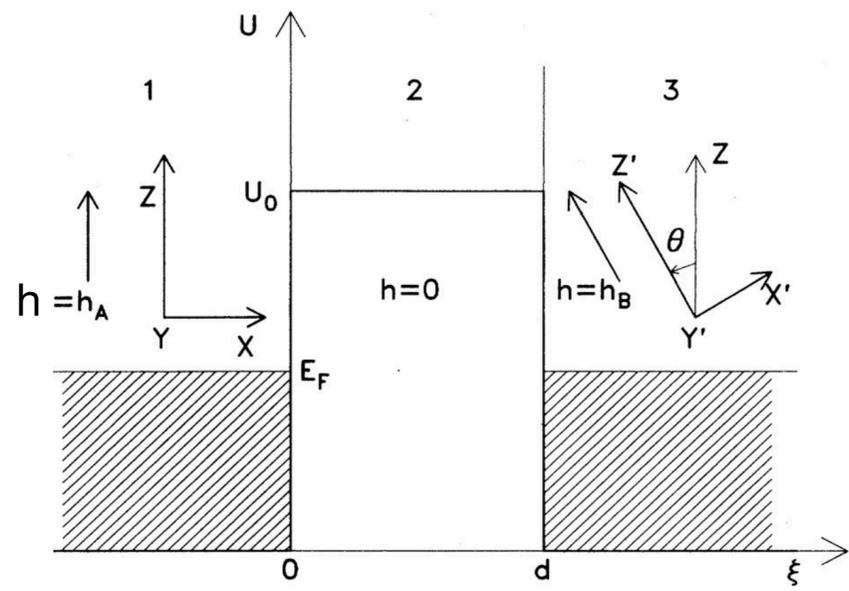


FIG. 6. Scheme of spin-vector dynamics due to the transverse terms of dissipative exchange coupling induced by an external voltage across the barrier.

### In magnetic metallic multilayers

J. C. Slonczewski, JMMM **159**, L1-L7 (1996)  
 L. Berger, PRB **54**, 9353 (1996)

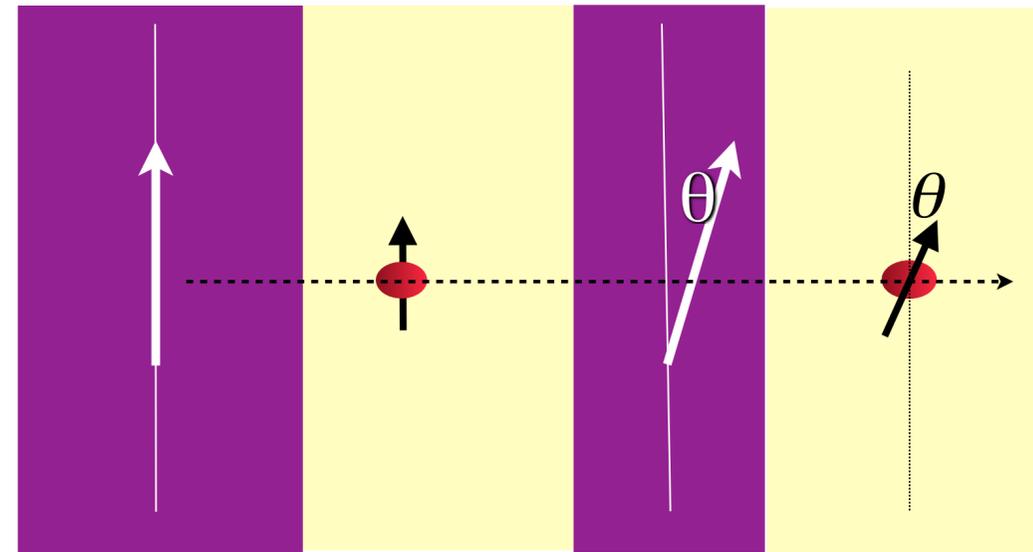
Applications: Magnetic Random Access Memory, STT-MRAM

Nature Nanotechnology, March 2015  
 Spin-transfer-torque memory



# Basic Physics of Spin Transfer

Based on conservation of angular momentum



$$\frac{d\vec{S}_{\text{int}}}{dt} \rightarrow \vec{\tau}$$

$$\left| \frac{d\vec{S}_{\text{int}}}{dt} \right| = \frac{\hbar}{2e} IP \sin \theta$$

$$\underbrace{\frac{1}{\gamma} \frac{d\vec{M}}{dt}}_{\text{magnetization}} + \underbrace{\frac{d\vec{S}_{\text{int}}}{dt}}_{\text{itinerant charge}} = 0$$

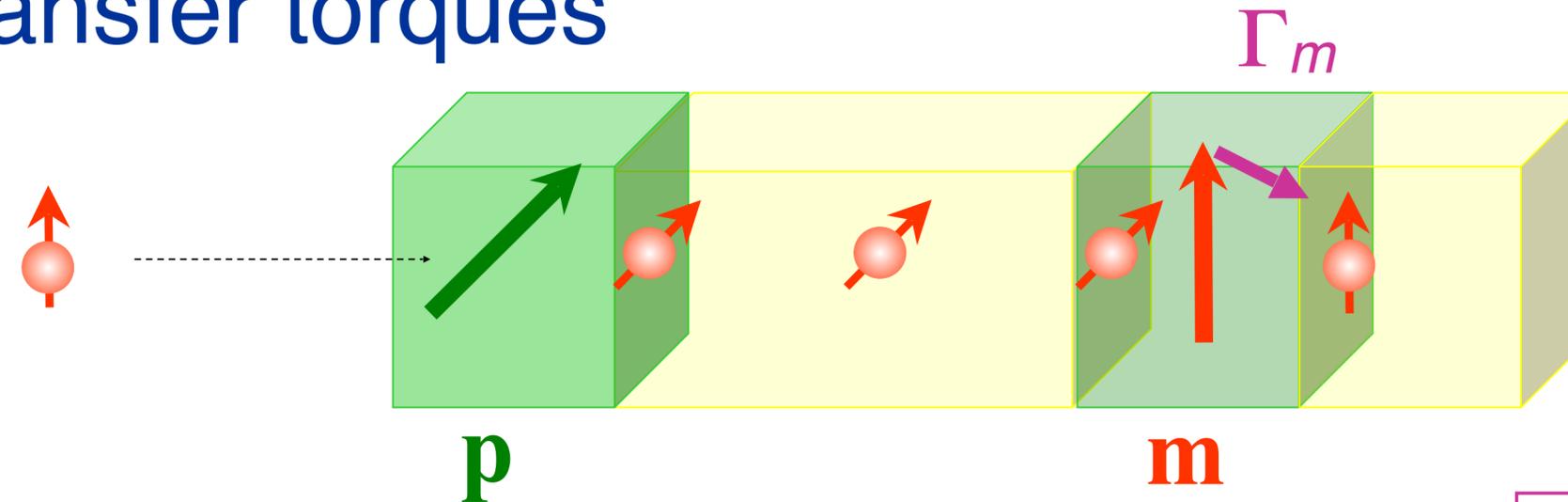
- ▶ Reference layer ‘sets’ spin-polarization of current
- ▶ Enables readout of magnetization state through the tunnel magnetoresistance (TMR), giant magnetoresistance (GMR), or anisotropic magnetoresistance (AMR) effects



# Basic Physics of Spin Transfer

Based on conservation of angular momentum

## Spin transfer torques



Animation courtesy of  
Eric Fullerton, UCSD

Angular momentum conservation  
spin transfer torques

$$\Gamma_m = \frac{dS_{\text{int}}}{dt}$$

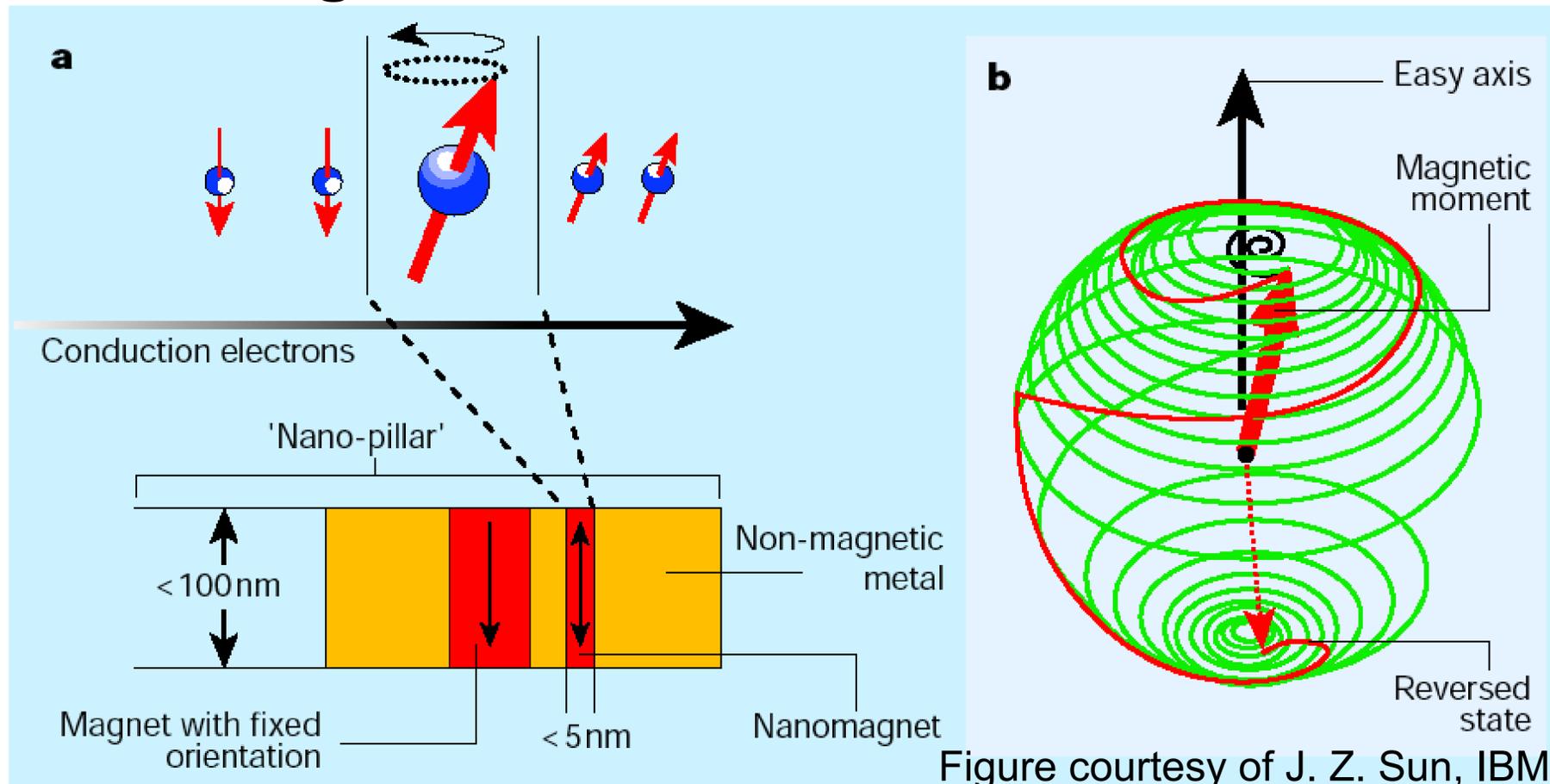
**All electrical** (no mechanical parts) fast magnetic memory device

- ▶ Reference layer 'sets' spin-polarization of current
- ▶ Enables readout of magnetization state through the tunnel magnetoresistance (TMR), giant magnetoresistance (GMR), or anisotropic magnetoresistance (AMR) effects

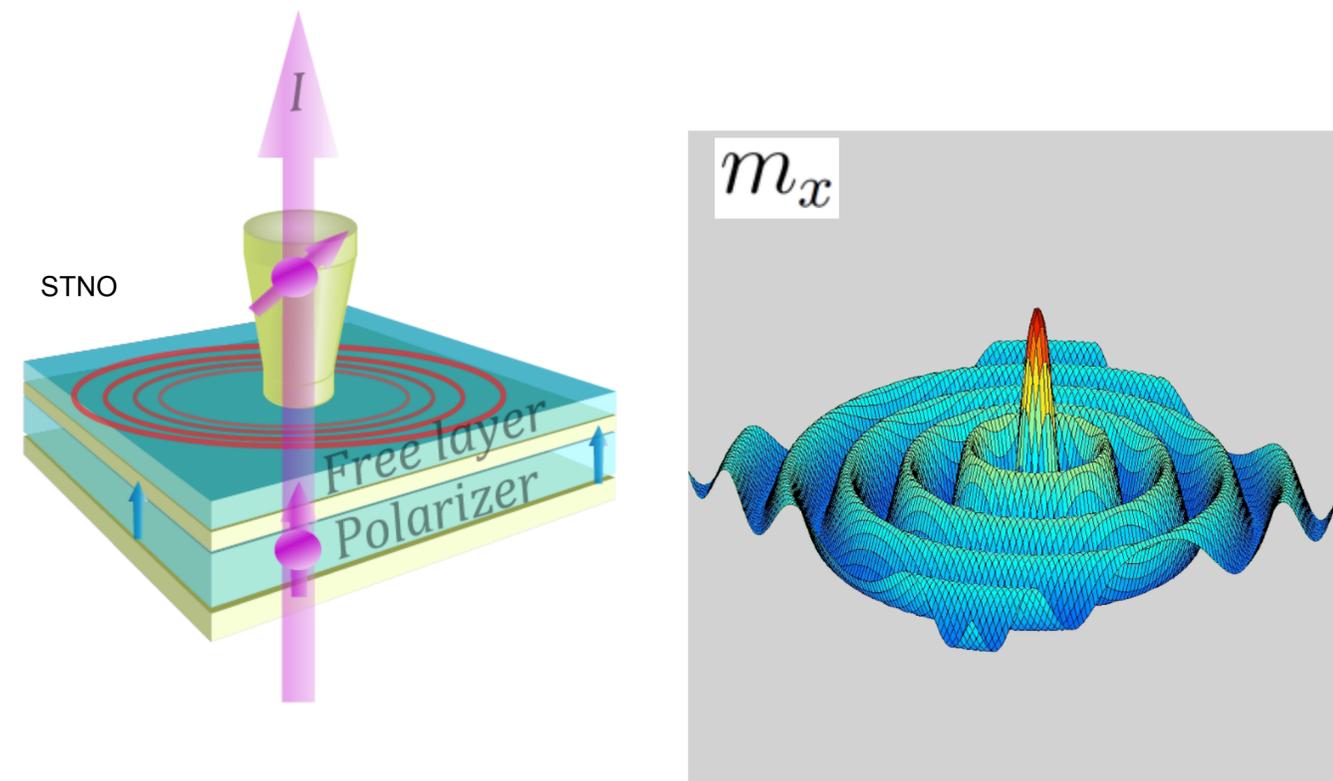


# Threshold Current for Magnetic Excitations

## Switching



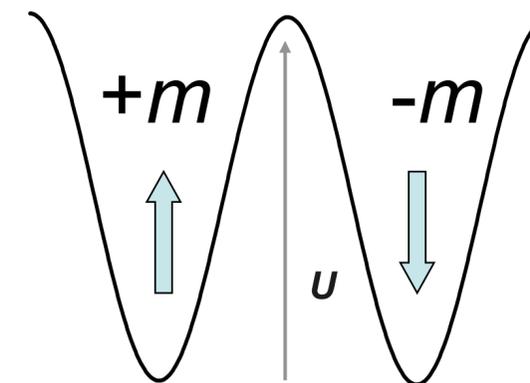
## Spin-wave excitations



Spin-current amplifies the motion for currents greater than a critical value:

“anti-damping switching” 
$$I_{c0} = \frac{2e}{\hbar} \frac{\alpha}{P} \mu_0 M_s H_k V = \frac{4e}{\hbar} \frac{\alpha}{P} U$$

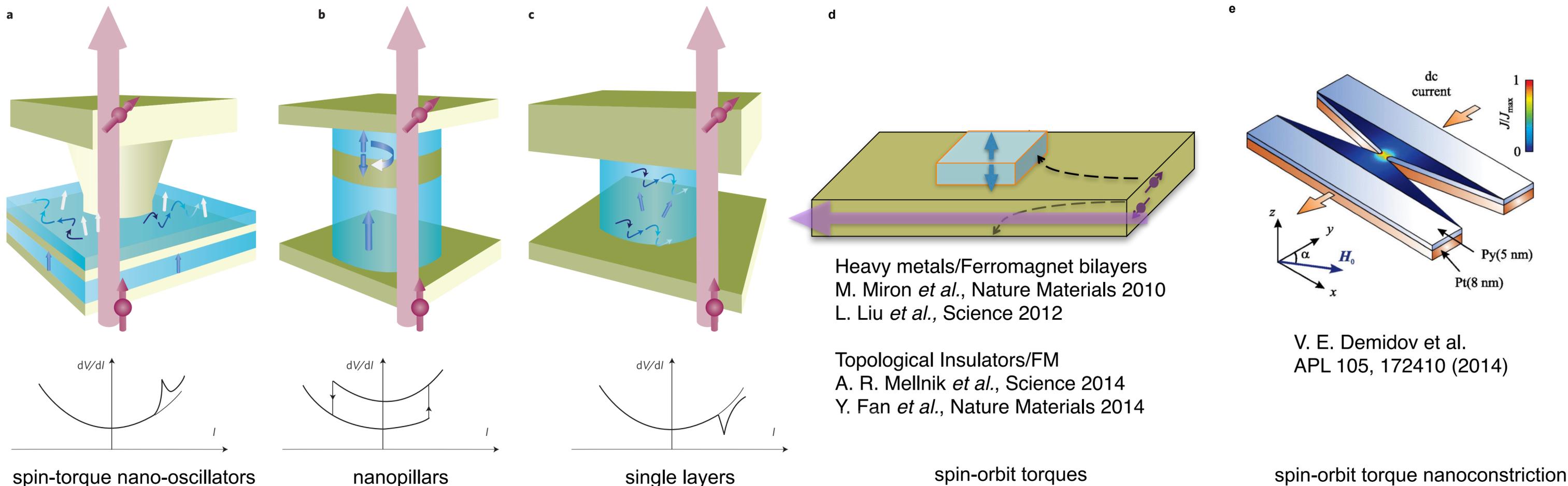
$P = 1, \alpha = 0.01, U = 60kT \rightarrow I_{c0} = 15 \mu A$





# Sample Geometries and Materials

Important in nanostructures: Large current densities+STT dominate over Oersted fields



from: A. Brataas, ADK, H. Ohno, Nature Materials 2012

$$\frac{d\hat{m}}{dt} = \gamma\mu_0\hat{m} \times \vec{H}_{\text{eff}} + \underbrace{\alpha\hat{m} \times \frac{d\hat{m}}{dt} + \gamma a_J \hat{m} \times (\hat{m} \times \hat{p})}_{\text{STT can compensate damping in regions in the material}}$$

STT can compensate damping in regions in the material

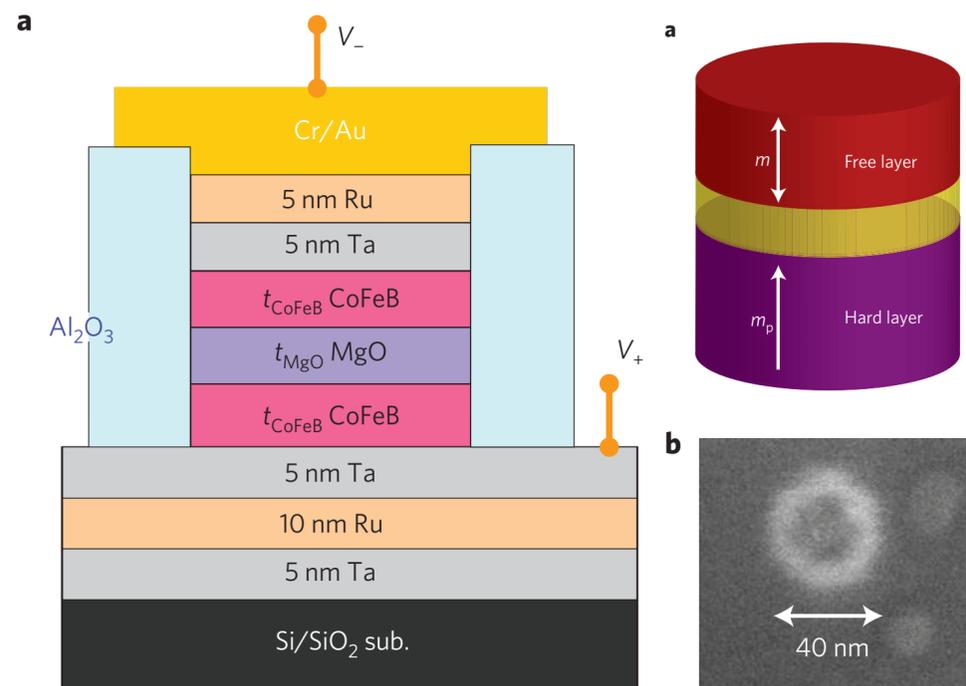
# Physics and Applications of Spin-Transfer Torques

## Outline

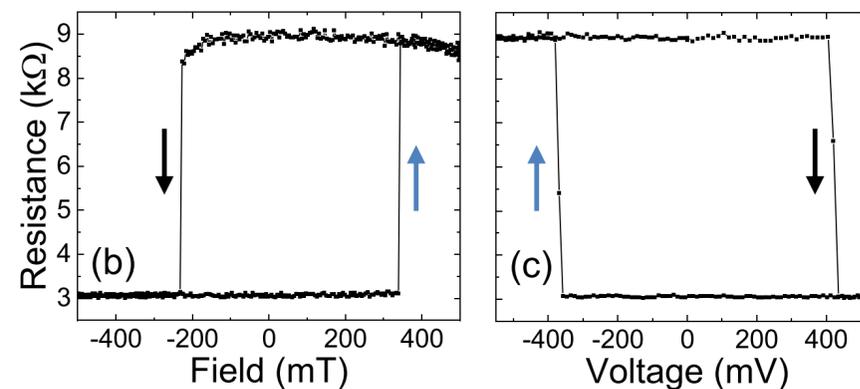
- Magnetic tunnel junctions and spin-transfer torques
- **Applications**
- Switching of magnetization, materials and device optimization
- Cryogenic applications

# A perpendicular-anisotropy CoFeB–MgO magnetic tunnel junction

S. Ikeda<sup>1,2\*</sup>, K. Miura<sup>1,2,3</sup>, H. Yamamoto<sup>1,2,3</sup>, K. Mizunuma<sup>2</sup>, H. D. Gan<sup>1</sup>, M. Endo<sup>2</sup>, S. Kanai<sup>2</sup>, J. Hayakawa<sup>3</sup>, F. Matsukura<sup>1,2</sup> and H. Ohno<sup>1,2\*</sup>



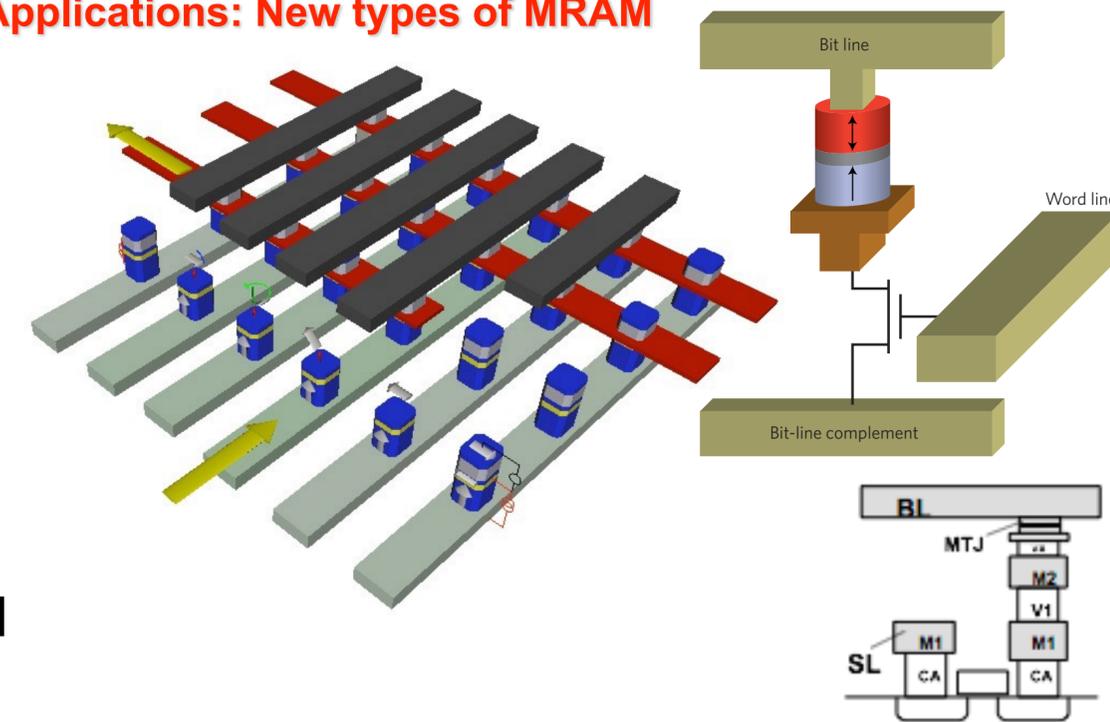
**Figure 1 | MTJ structure.** **a**, Schematic of an MTJ device for TMR and CIMS measurements. **b**, Top view of an MTJ pillar taken by scanning electron microscope.



Field induced free layer switching

Current-induced switching

Applications: New types of MRAM



R. Beach et al., IEDM 2008

Also, D.C. Worledge *et al.*, Applied Physics Letter **98**, 022501 (2011)

Perspective: A. D. Kent, Perpendicular all the way, Nature Materials **9**, 699 (2010)



# Memory Comparisons

	SRAM	eDRAM	DRAM	eFlash (NOR)	Flash (NAND)	FeRAM	PCM	STT MRAM	SOT MRAM	RRAM
<b>Endurance</b>	Unlimited	Unlimited		$10^5$		$10^{14}$	$10^9$	Unlimited	Unlimited	$10^9$
<b>Read/Write access time</b>	< 1 ns	1-2 ns	30 ns	10/ $10^3$ ns	100/ $10^6$ ns	30 ns	10/100 ns	2-30 ns	2-30 ns	1-100 ns
<b>Density</b>	Low (6 transistors)	Medium		Medium	High (multiple bits/cell)	Low (limited scalability)	High (multiple bits/cell)	Medium	Medium (>STT MRAM)	High (multiple bits/cell)
<b>Write power</b>	Medium	Medium		High		Medium	Medium	Medium	Low	Medium
<b>Standby power</b>	High	Medium		Low		Low	Low	Low	Low	Low
<b>Other</b>	Volatile	Volatile. Refresh power and time needed.		High voltage required		Destructive readout	Operating T < 125 C	Low read signal	Fabrication challenges	Complex mechanism

Comparison of key features of existing and emerging memories. Significant disadvantages are marked in red. Estimates for emerging memories are based on expectations for functioning chips, not demonstrations of individual bits.

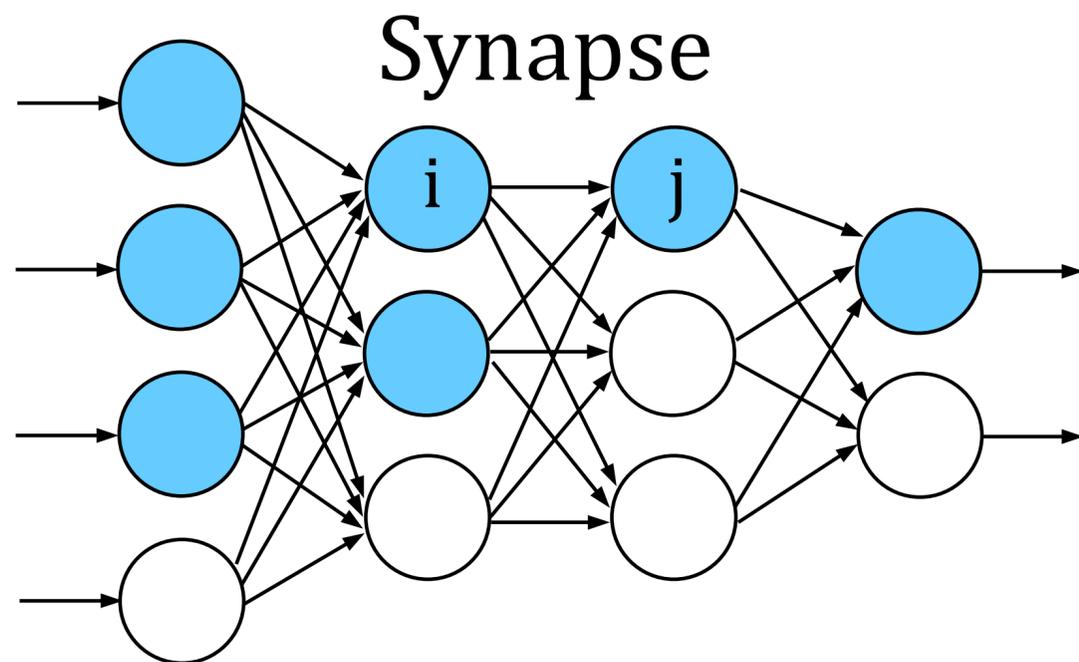
From A. D. Kent and D. C. Worledge, "A new spin on magnetic memories," Nature Nanotechnology **10**, 187 (2015)



# Convolutional Neural Networks

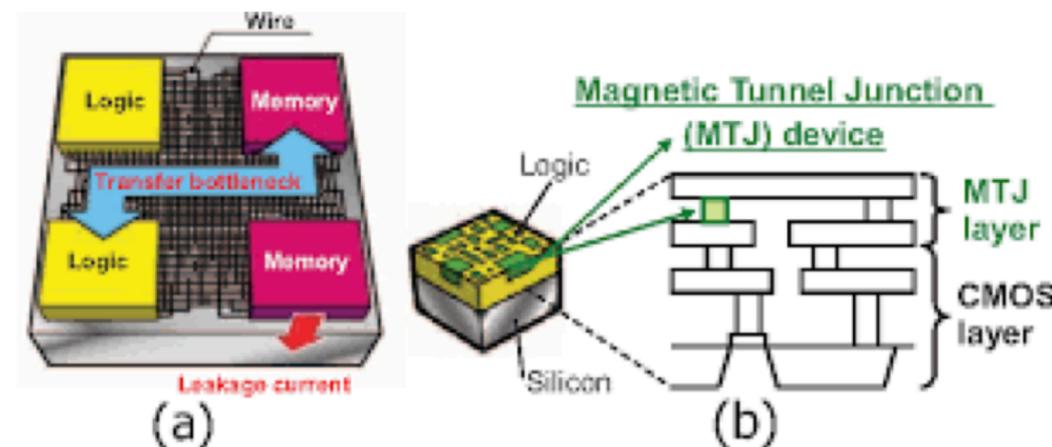
## Some potential applications of MTJs

Neuron



Spin transfer torque magnetic random access memory used to store weights in a convolutional neural network

- Persistent (i.e. nonvolatile)
- Energy needed only for write/read
- Closely integrated with logic elements



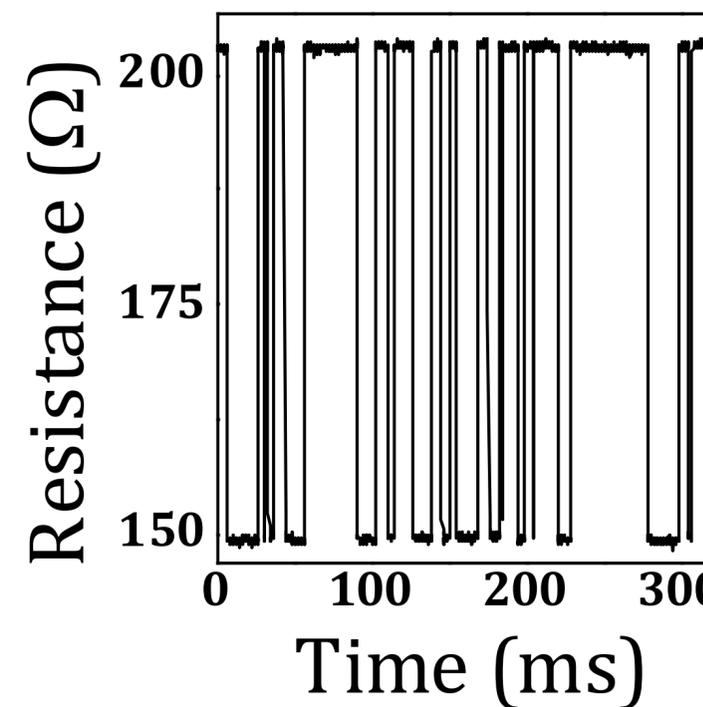
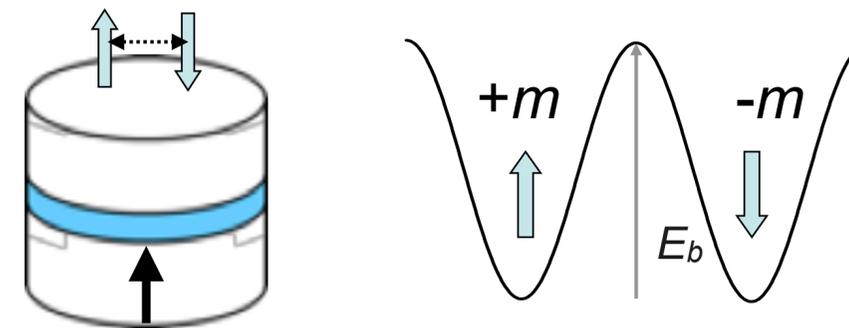
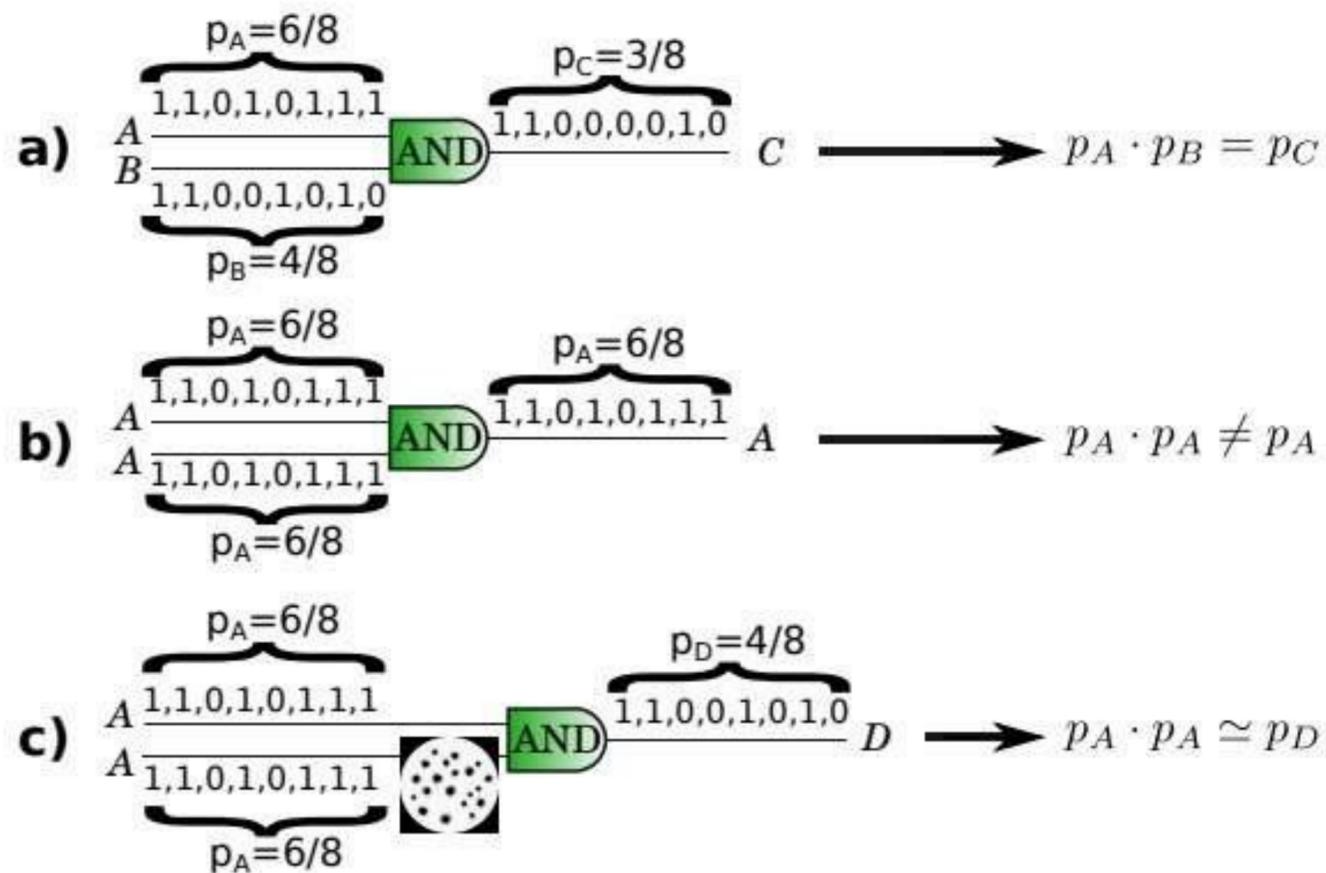
From: T. Hanyu et al., Design, Automation & Test in Europe Conference 2015  
DOI:10.7873/date.2015.1119



# Stochastic Computing

## Approximate computing

## MTJ random number generator



$$E_b / (kT) \lesssim 20$$

D. Pinna *et al.*, Phys. Rev. Applied 9, 064018 (2018)

Spin transfer and spin-orbit torques can set:

- Probabilities
- Time scales

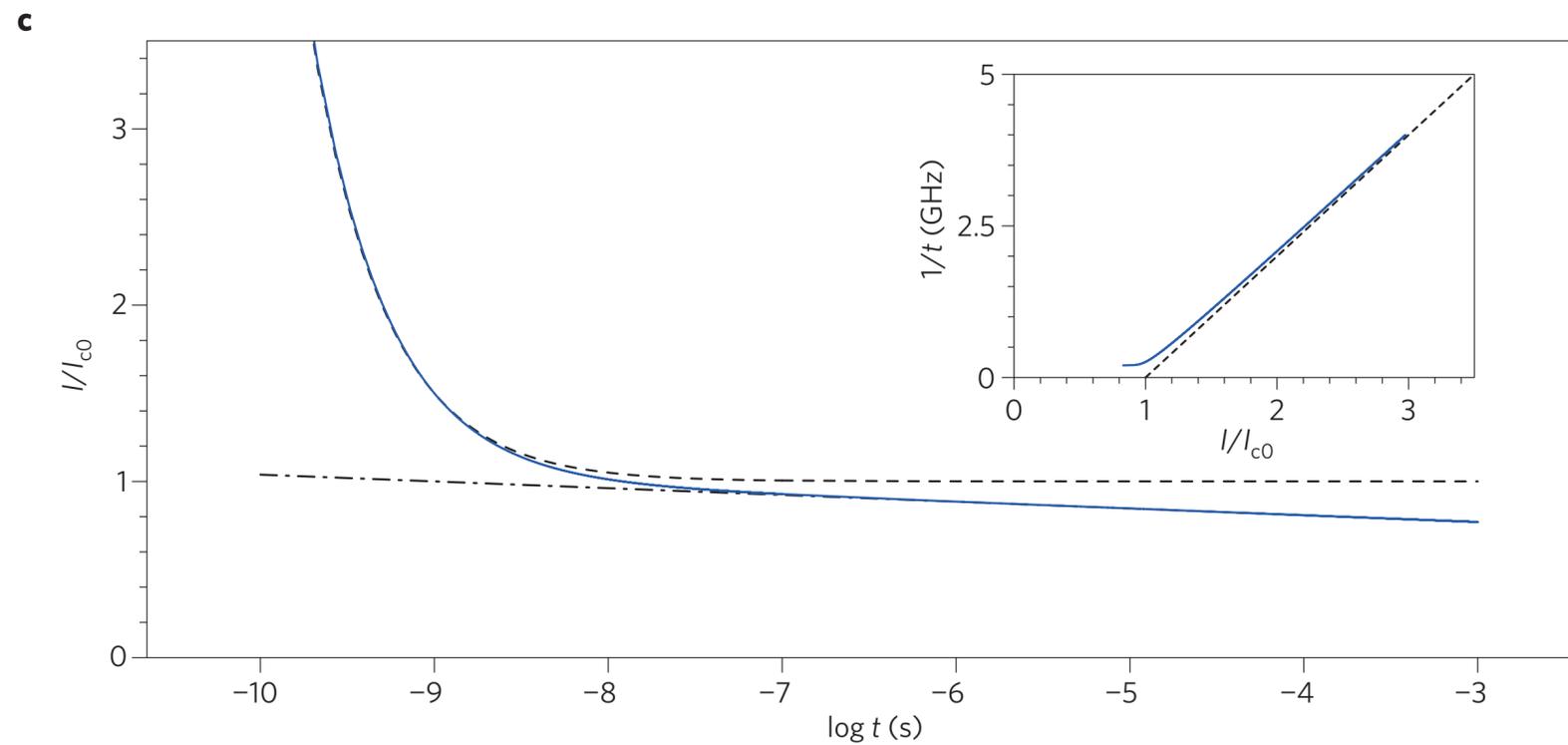
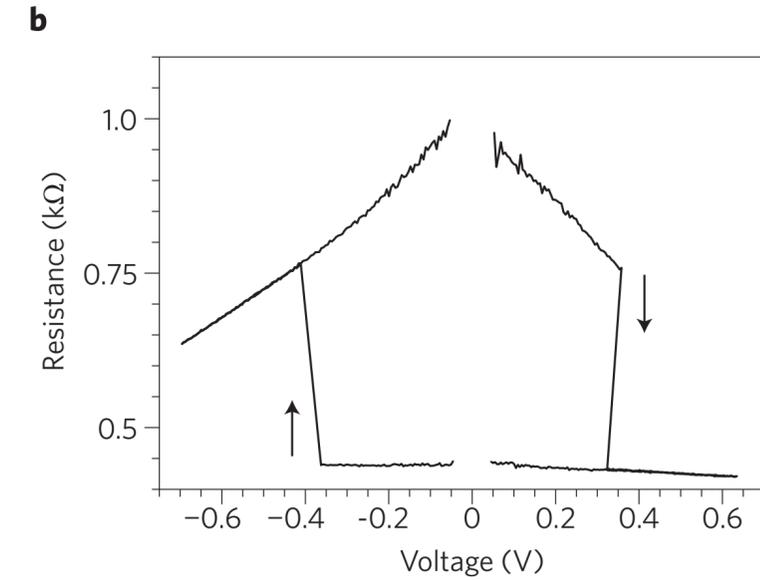
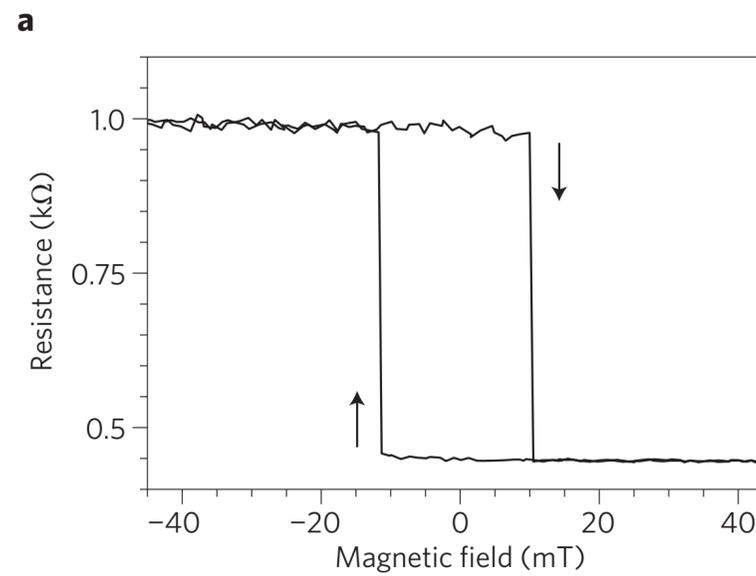
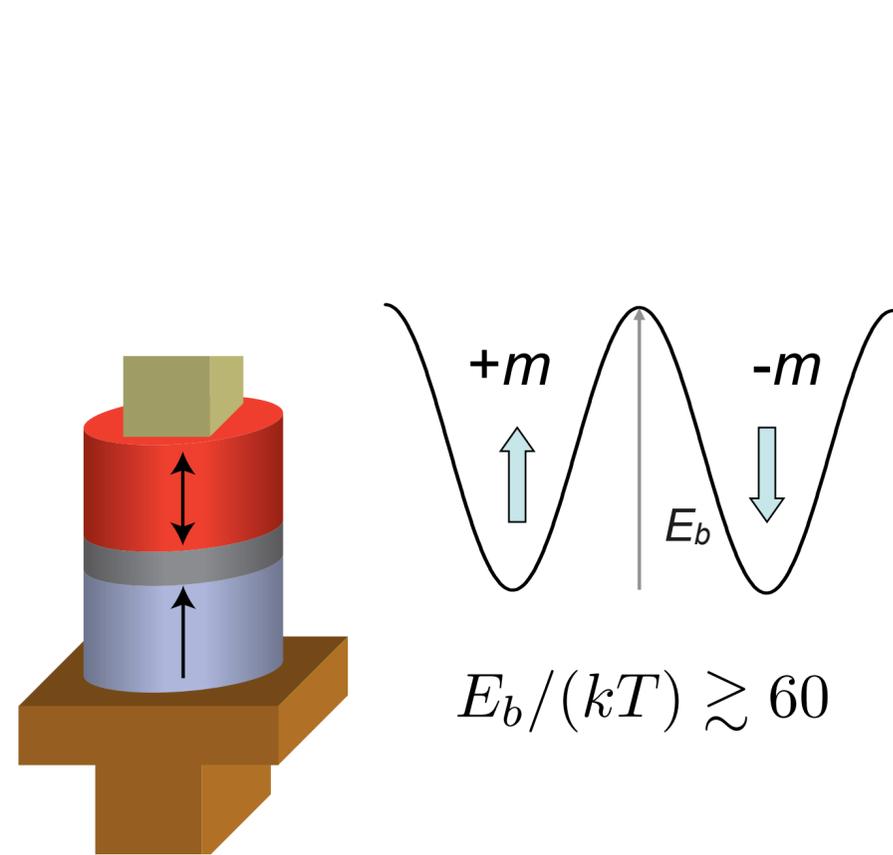
# Physics and Applications of Spin-Transfer Torques

## Outline

- Magnetic tunnel junctions and spin-transfer torques
- Applications
- **Switching of magnetization, materials and device optimization**
- Cryogenic applications



# Magnetic Tunnel Junction



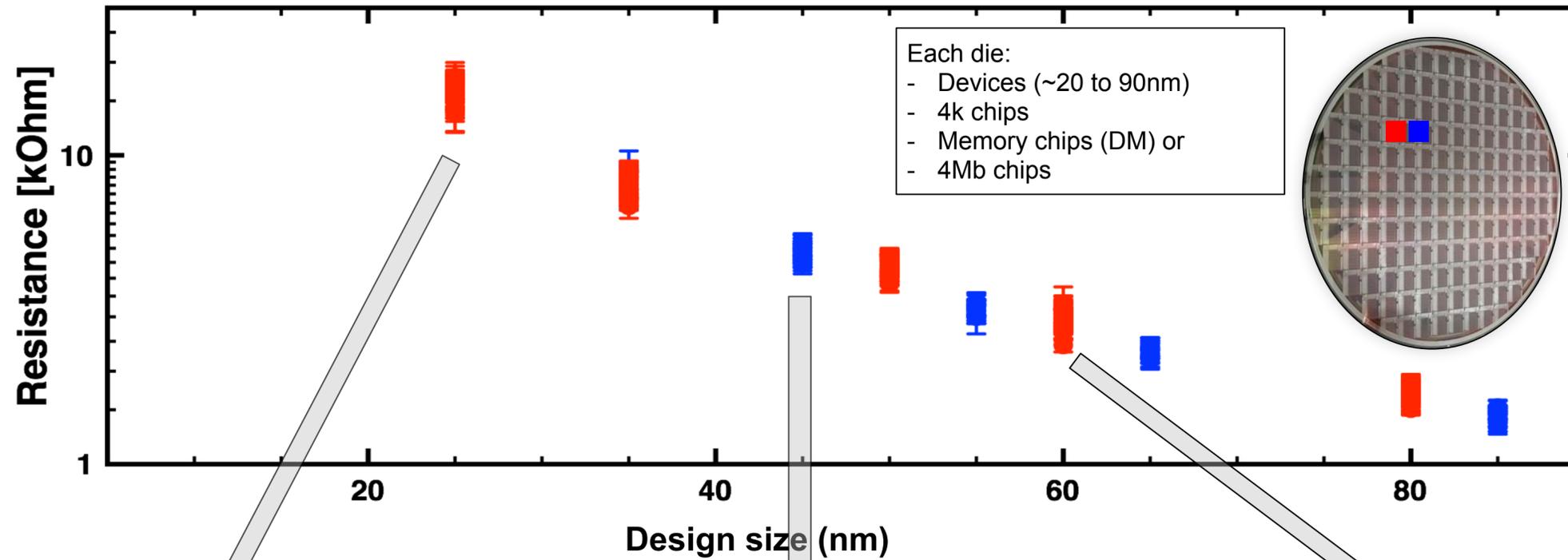
A. D. Kent and D. C. Worledge, "A new spin on magnetic memories," *Nature Nanotechnology* **10**, 187 (2015)

# MRAM Technology Development at Spin Memory

MTJ nanopillars for Gbit density arrays

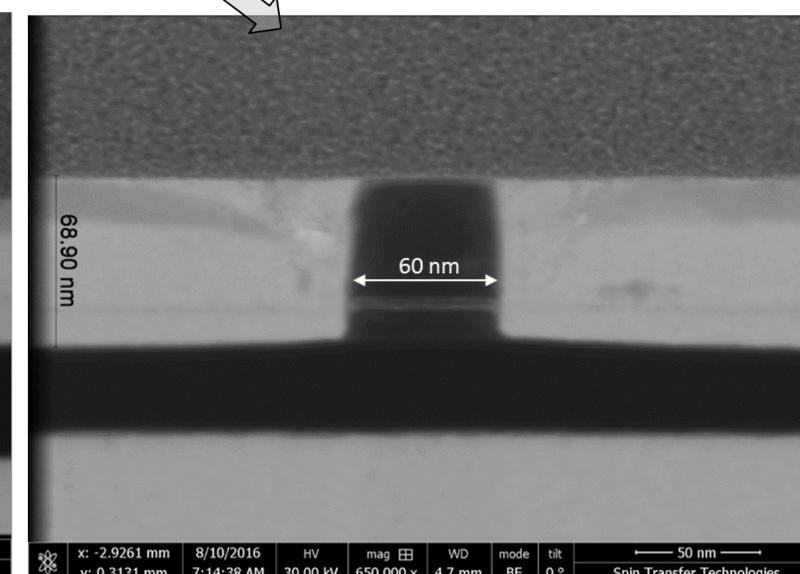
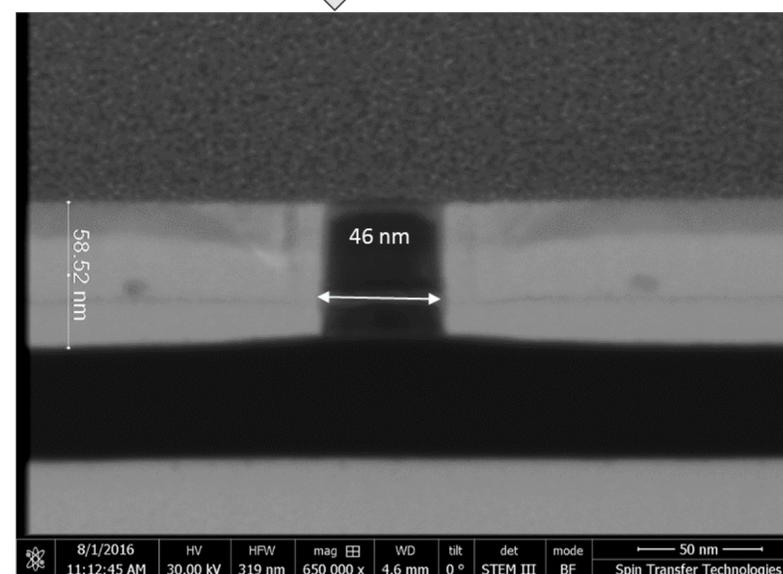
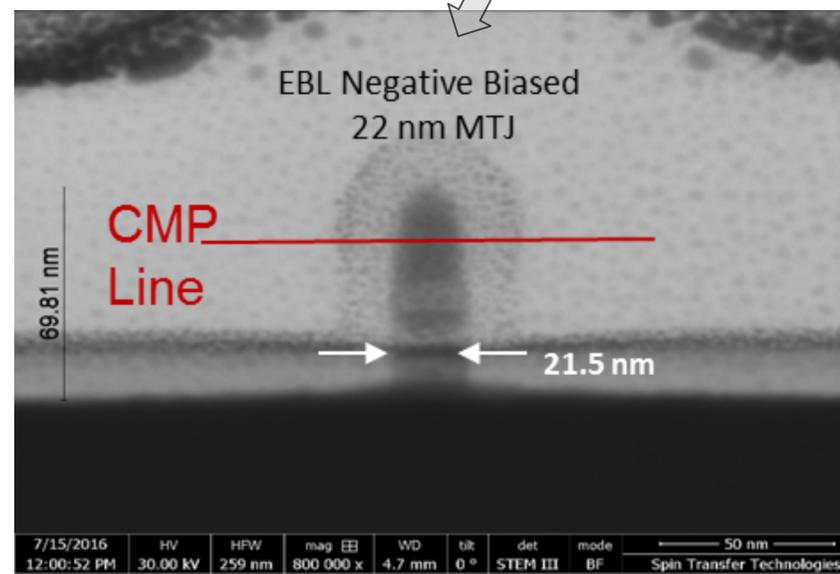


- Scaling down to 20 nm diameters



Two e-beam exposures were used in checkerboard pattern

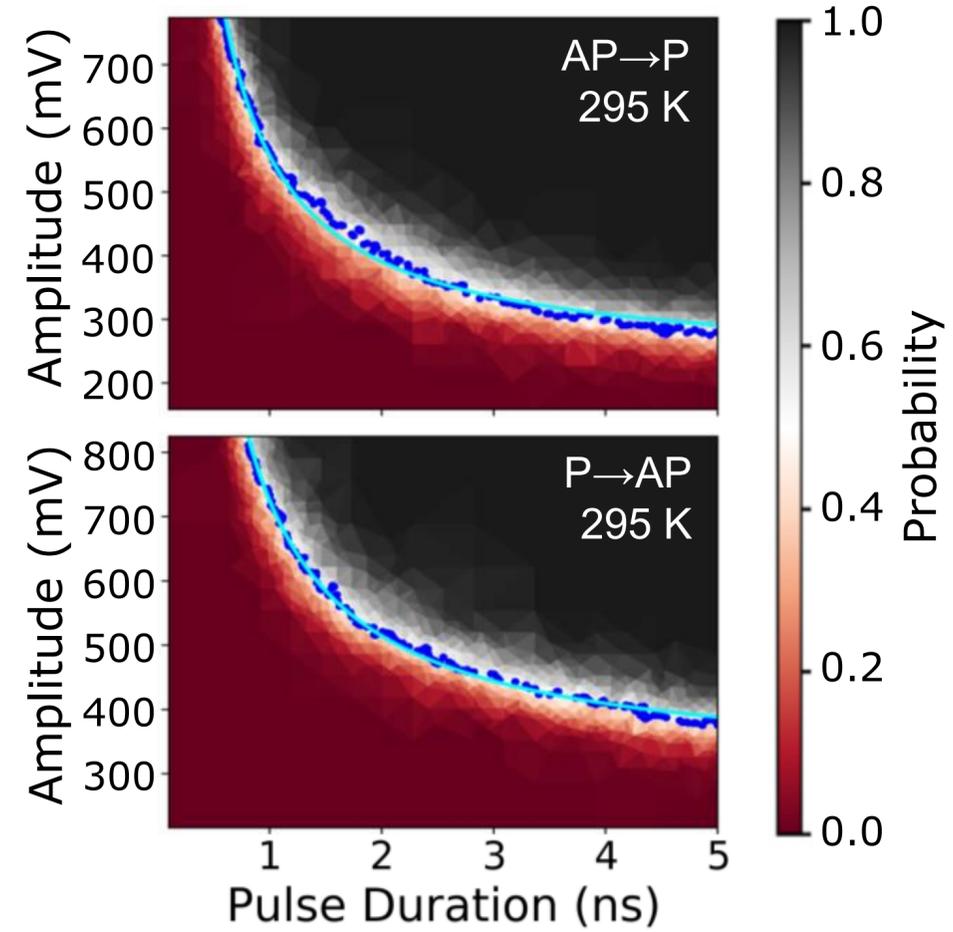
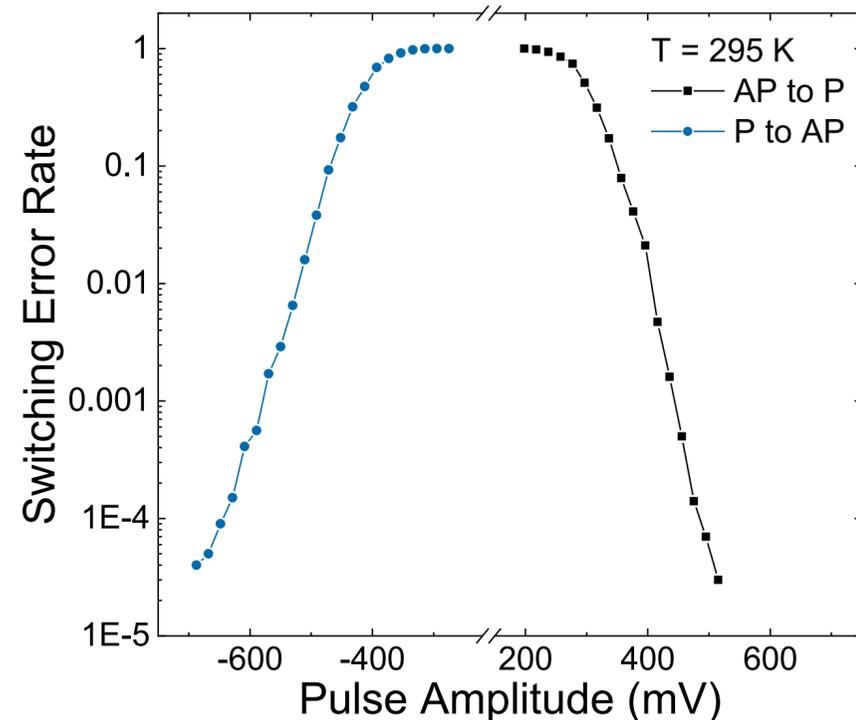
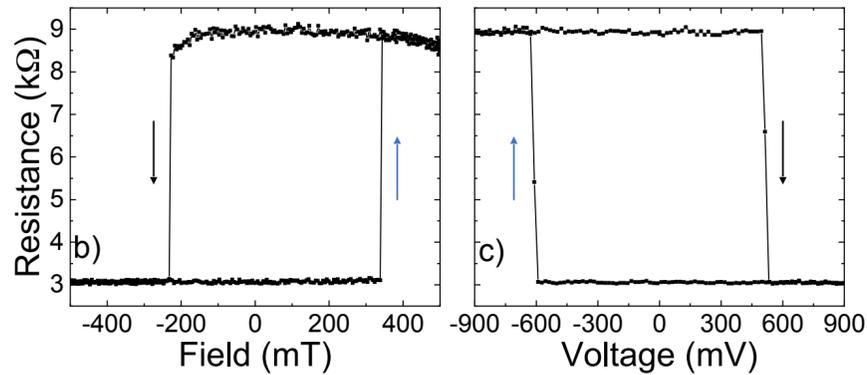
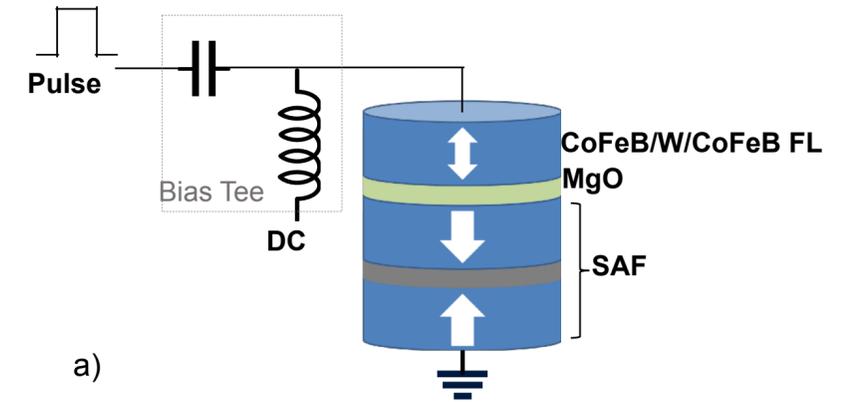
Slide courtesy of Mustafa Pinarbasi, CTO, Spin Memory





# High Speed Magnetization Switching

40 nm diameter nanopillar



$$\frac{1}{\tau} = \frac{1}{\tau_0} \left( \frac{I - I_c}{I_c} \right)$$

$$\tau_0 I_c = I\tau - I_c\tau$$

const.      N      dissipation

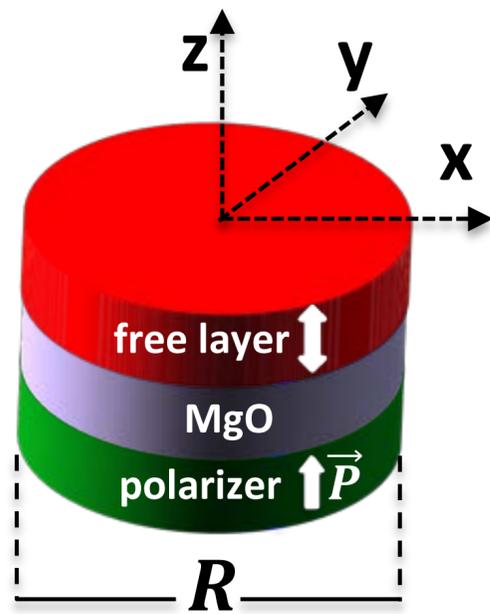
Write energy:  $\lesssim 250$  fJ

Laura Rehm *et al.*, APL **115**, 182404 (2019)

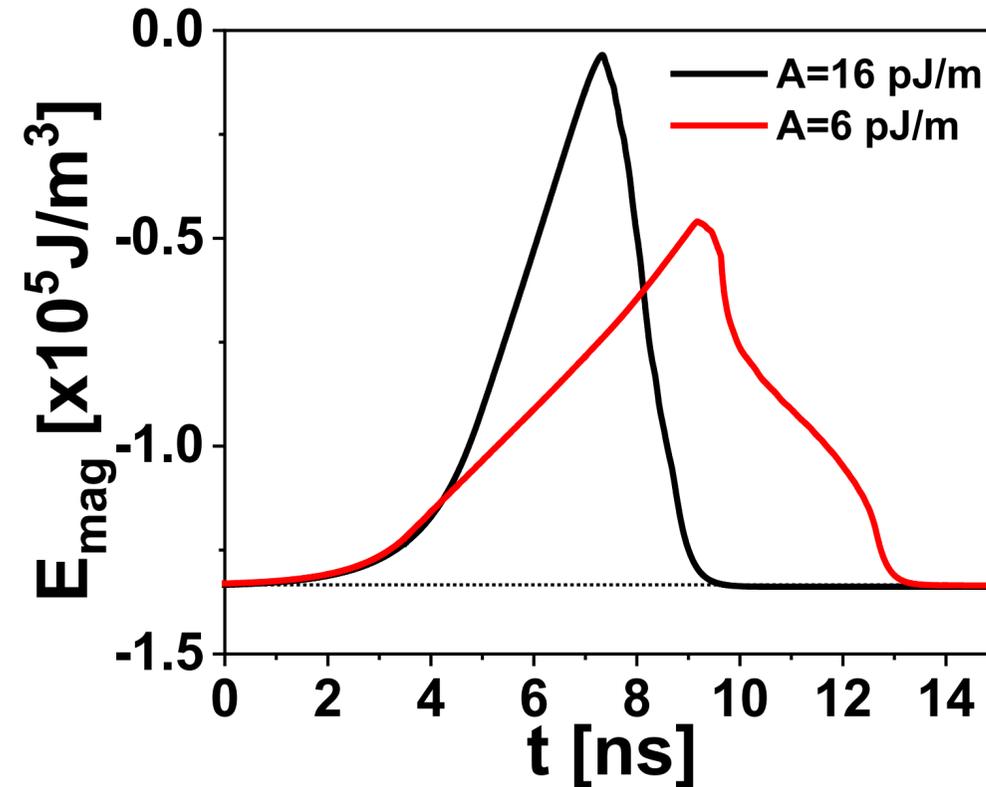
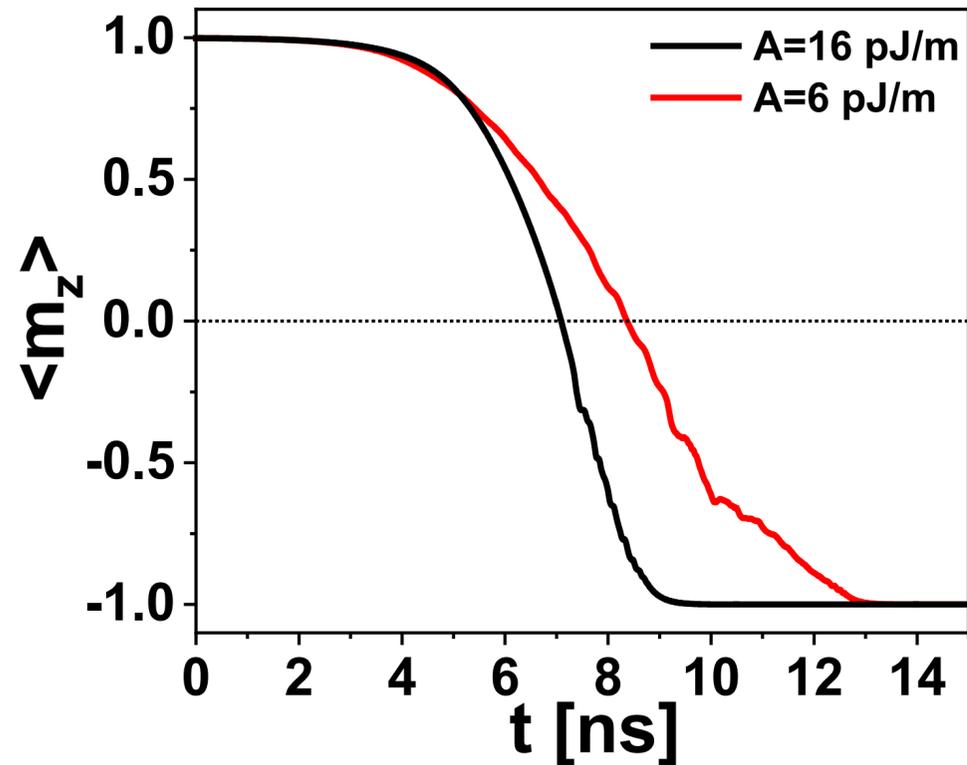


# Magnetic Anisotropy and Exchange Energy

- Set the length scales for spatial variation of the magnetization
- Determines the energy barrier for thermally activated magnetization reversal and affects the **switching time**



$R = 100 \text{ nm}$   
 $J/J_{c0} = 1.6$

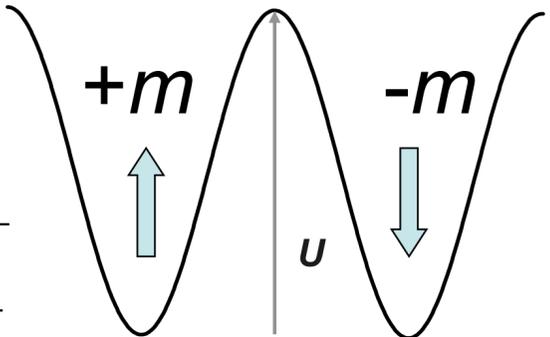


Effective anisotropy:  $\mu_0 M_{\text{eff}} = 0.3 \text{ T}$  } domain wall width:  $\Delta = 20 \text{ nm}$   
 Exchange constant:  $A = 16 \text{ pJ/m}$



# Magnetic Anisotropy and Exchange Energy

- Set the length scales for spatial variation of the magnetization
- Determines the **energy barrier for thermally activated magnetization reversal** and affects the switching time

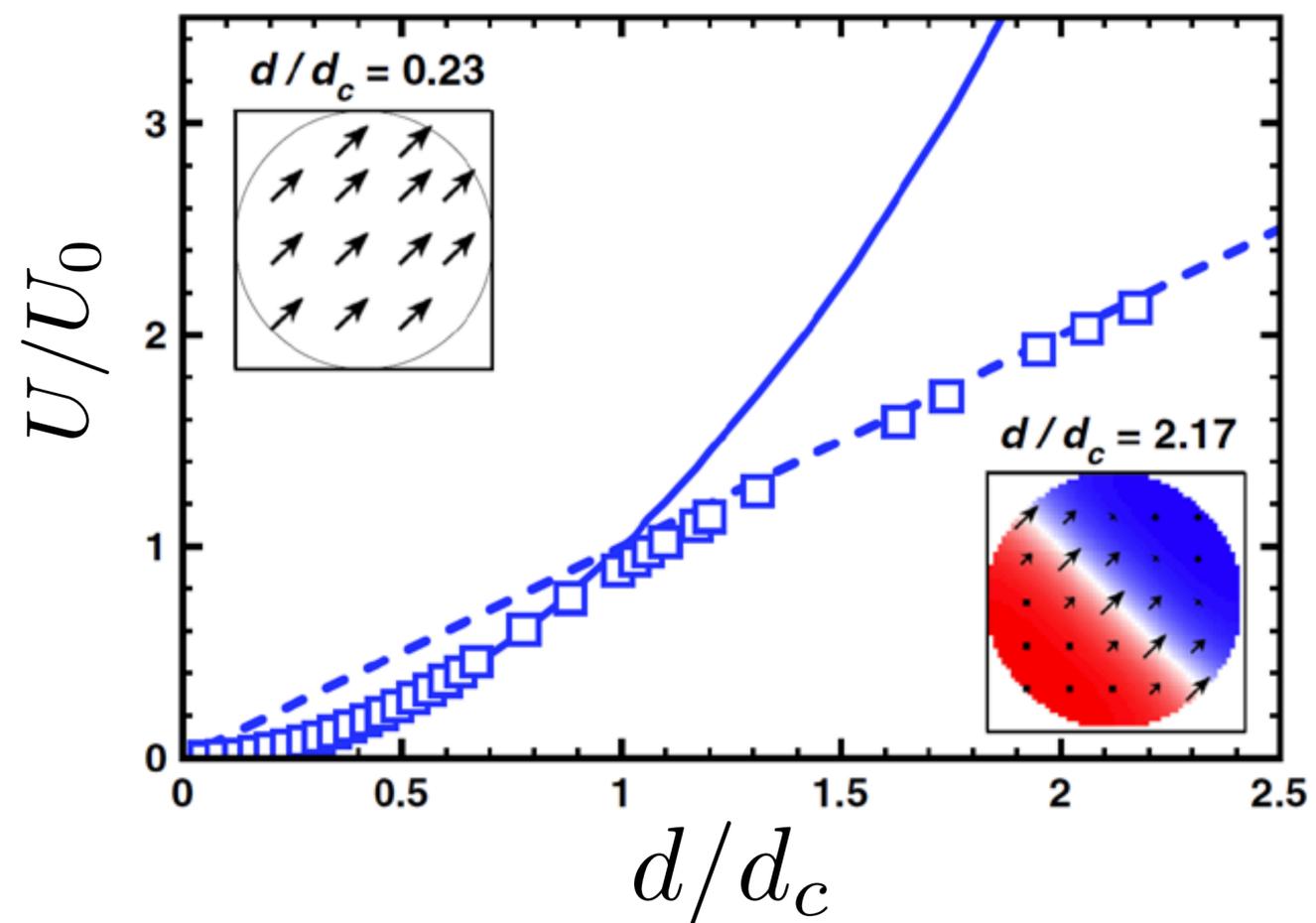


$$d_c = \frac{16}{\pi} \sqrt{\frac{A}{K_{\text{eff}}(d)}}$$

$$d \leq d_c \quad U = K_{\text{eff}} \frac{\pi}{4} d^2 t$$

$$d > d_c \quad U = 4 \sqrt{AK_{\text{eff}}} dt$$

$A$  : exchange constant  
 $K_{\text{eff}}$  : effective perpendicular anisotropy  
 $d$  : diameter of the element  
 $t$  : thickness



Gabriel D. Chaves-O'Flynn *et al.*, Phys. Rev. Applied 4, 024010 (2015)

Experiment: L. Thomas *et al.*, IEDM 15-673 (2015)

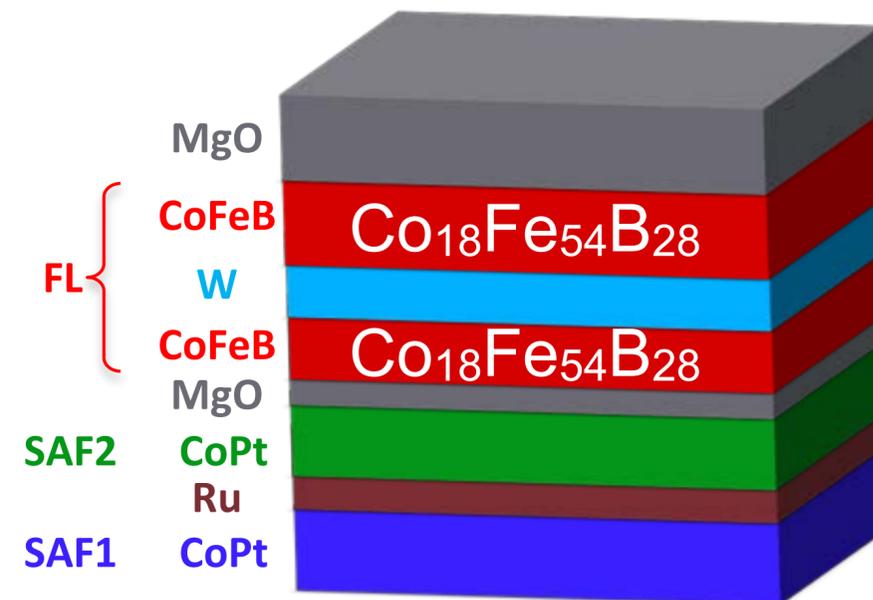


# Magnetic Anisotropy and Exchange Energy

- **Free layer in pMTJ are composite layers**

-Non-magnetic layers are inserted to:

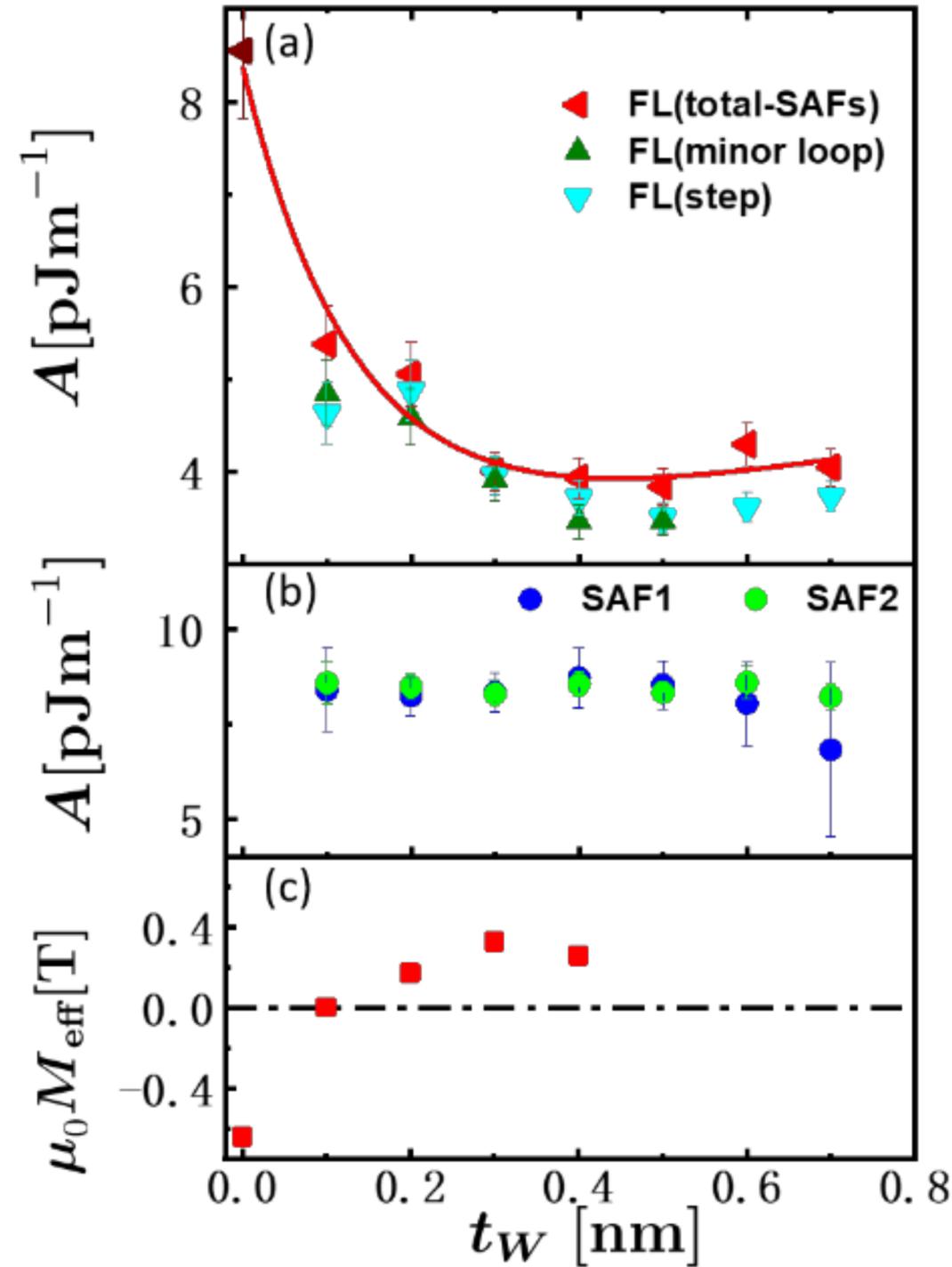
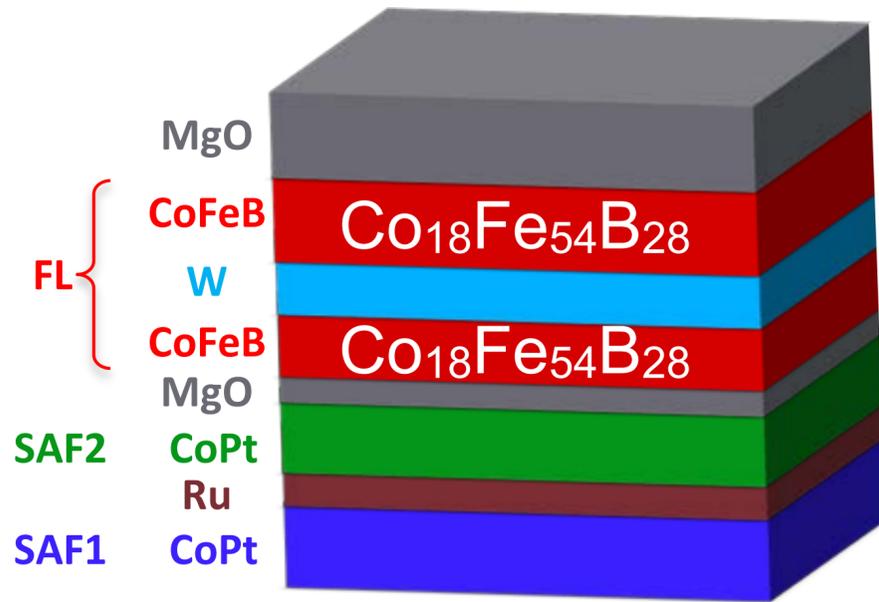
- Increase the perpendicular magnetic anisotropy (i.e. add interfaces and interface magnetic anisotropy)
- Enable increased layer thickness and thus magnetic volume to increase the magnetic stability



- We did experiments to determine the exchange constant and magnetic anisotropy of CoFeB/W/CoFeB composite free layers as a function of the tungsten insertion layer thickness.



# Magnetic Anisotropy and Exchange Energy



$$K_{\text{eff}} = K_p - \frac{\mu_0 M_S^2}{2}$$

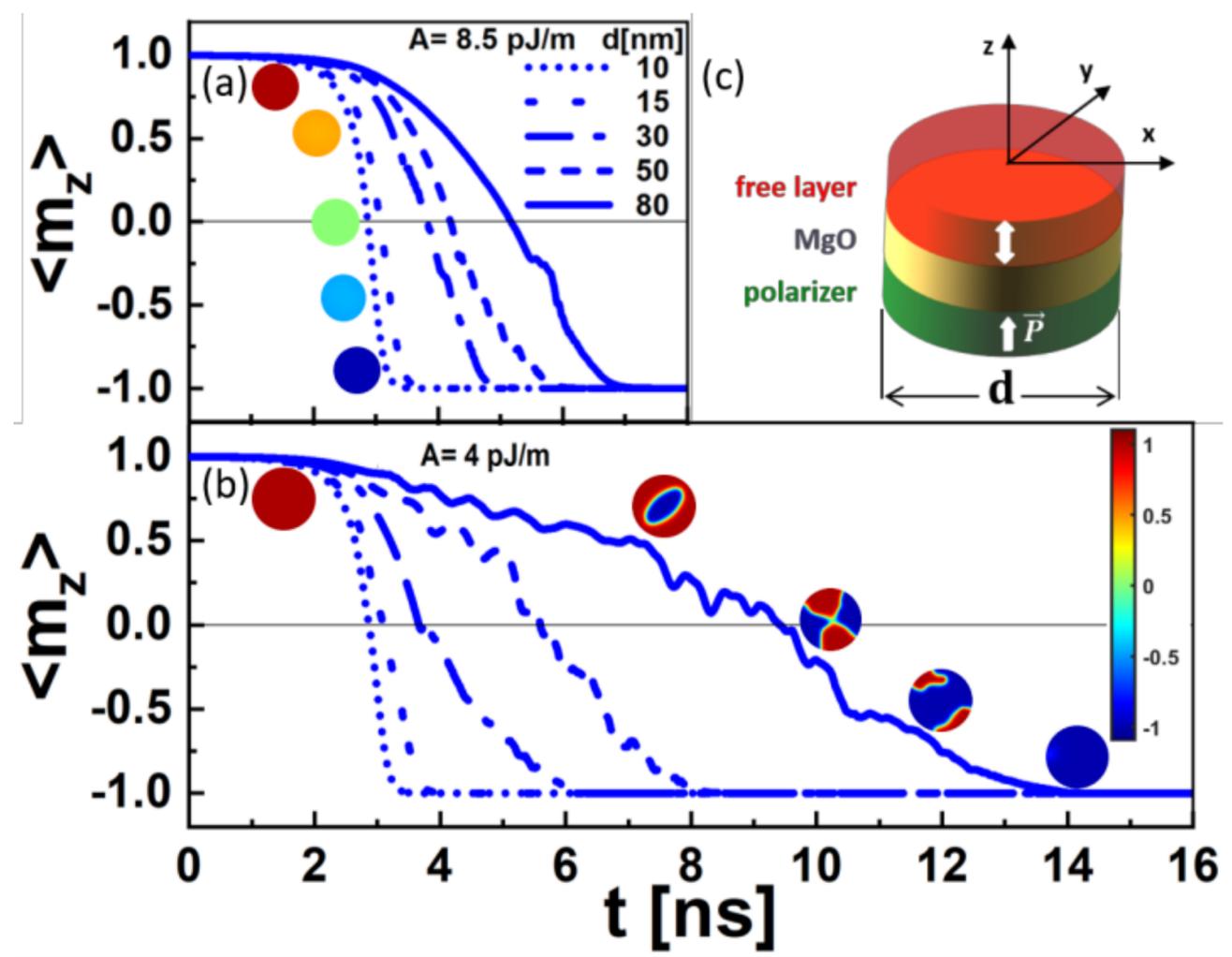
$$M_{\text{eff}} = \frac{2K_{\text{eff}}}{\mu_0 M_S}$$

Jamileh Beik Mohammadi *et al.*, "Reduced Exchange Interactions in Magnetic Tunnel Junction Free Layers with Insertion Layers," ACS Appl. Electron. Mater **1**, 2025 (2019)

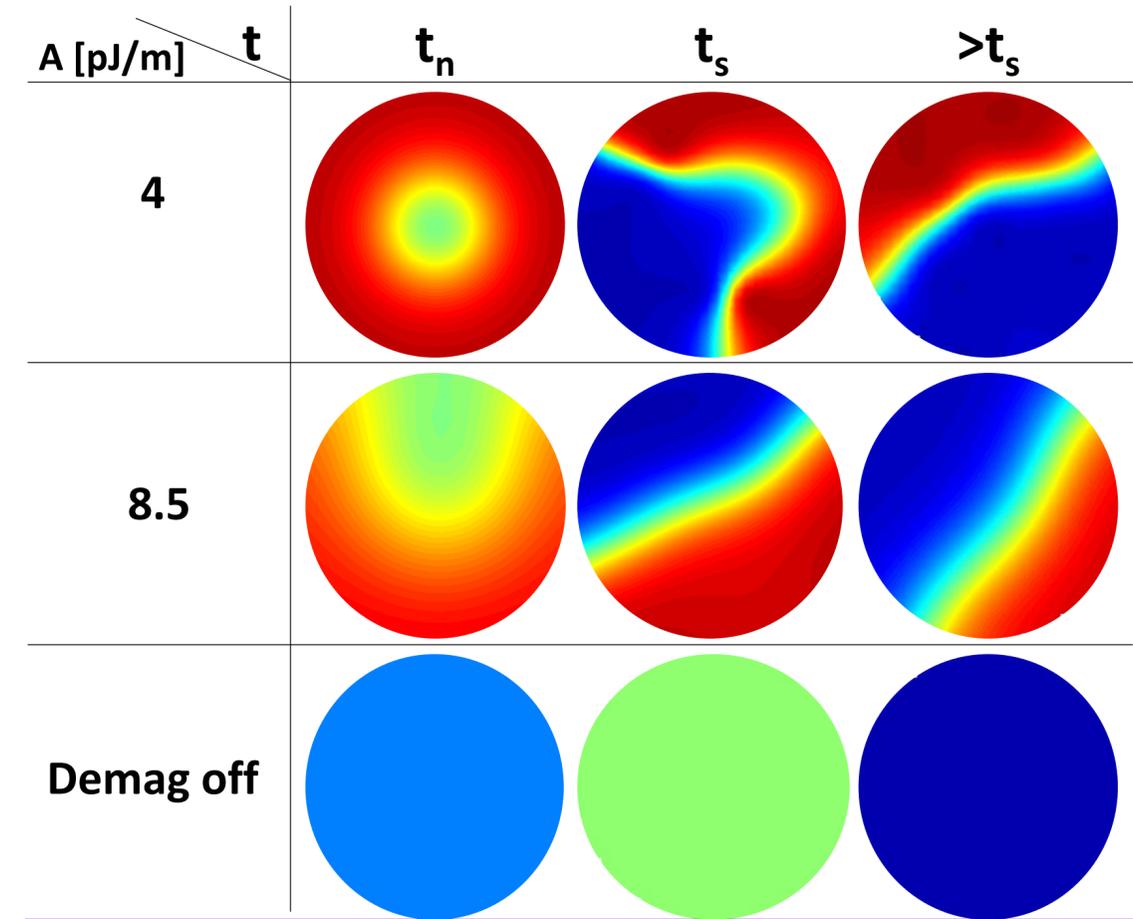


# Micromagnetic Modeling

Magnetization vs time



Switching process



$t_n$ : nucleation time  
 $t_s$ : switching time,  $m_z=0$

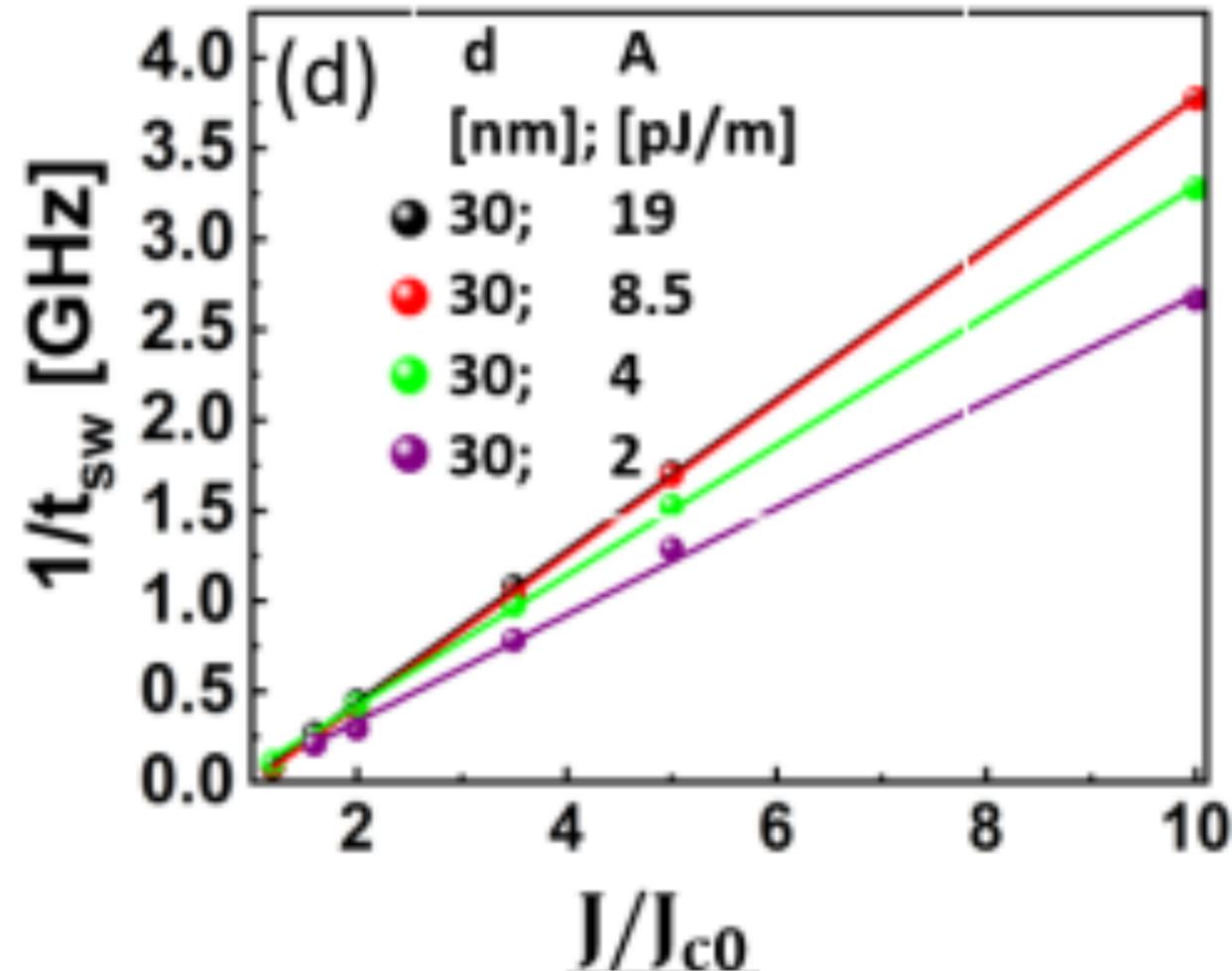
**Switching process:**

- Reversal in the center of the disk (formation of a reversed droplet)
- Reversed area moves to intersect the boundary (droplet drift instability)
- Domain wall formed that traverses the element
- Reversal by domain wall motion

see also, P. Bouquin *et al.*, APL 2018



## Switching speed



$t_s$ : switching time,  $m_z=0$

$$\frac{1}{\tau} = \frac{1}{\tau_0} \left( \frac{I - I_c}{I_c} \right)$$

## Switching speed:

- Switching rate is proportional to the current, independent of exchange constant
- Switching rate at fixed overdrive increases with increasing exchange constant

J. B. Mohammadi and AD. D. Kent, "Spin-torque switching mechanisms of perpendicular magnetic tunnel junctions nanopillars," arXiv:2003.13875 (2020).

see also, P. Bouquin *et al.*, APL 2018

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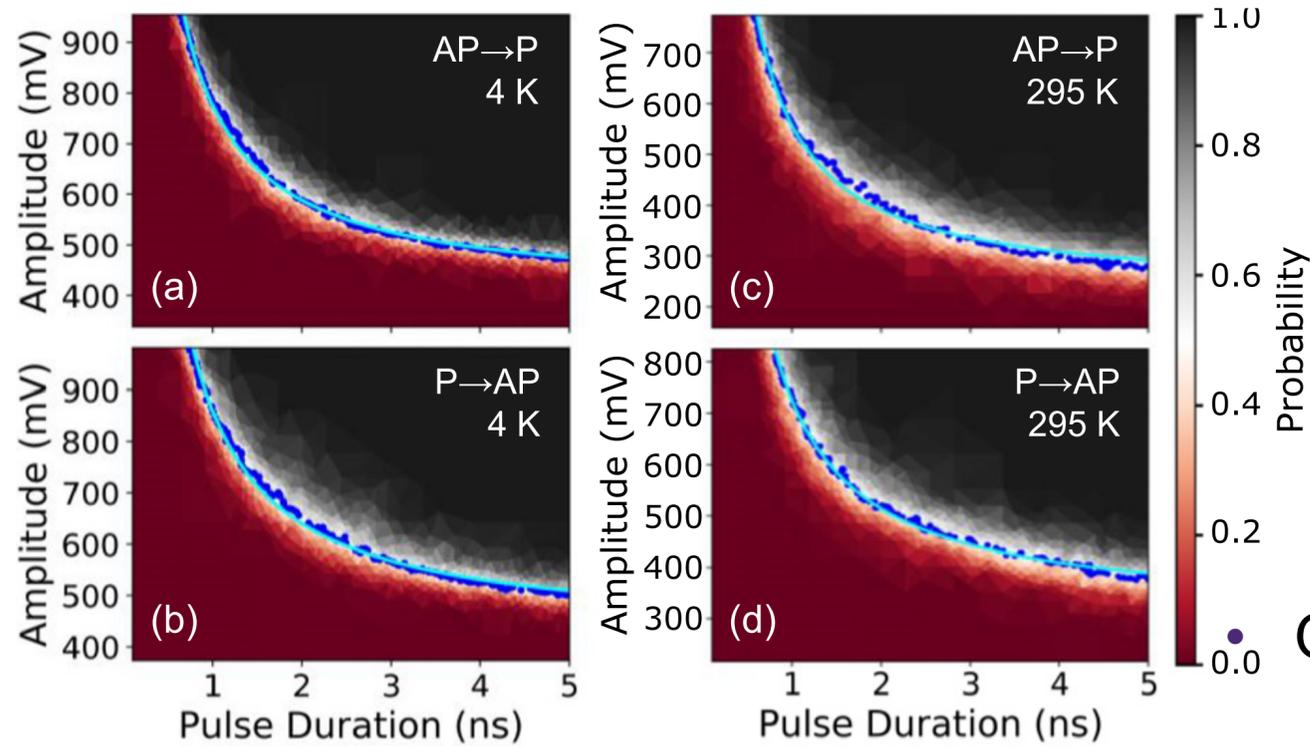
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# Cryogenic Memory

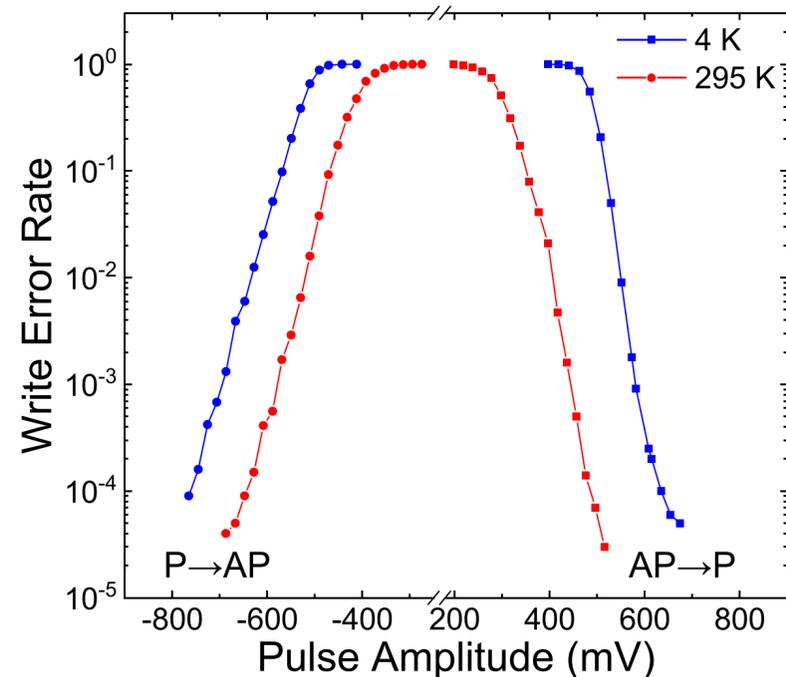
## Switching speed

## Switching energy



T (K)	$V_c$ (mV)		$\tau_0$ (ns)		$E$ (fJ)	
	AP→P	P→AP	AP→P	P→AP	AP→P	P→AP
4	399	421	0.94	1.03	<b>103</b>	<b>286</b>
75	393	416	0.94	1.05	<b>98</b>	<b>283</b>
150	381	403	0.96	1.1	<b>94</b>	<b>287</b>
295	225	305	1.48	1.38	<b>51</b>	<b>195</b>

Optimal write energy increases with decreasing temperature  
 ➤ Thermal energy reduces device switching energy



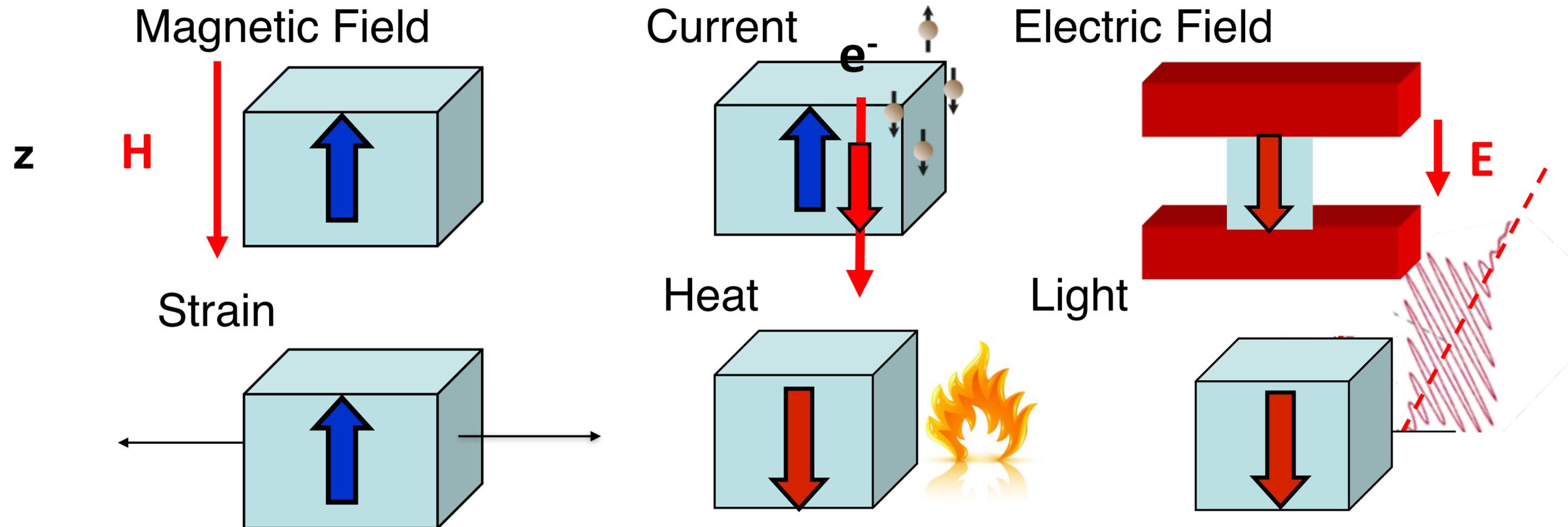
- Comparison to already studied cryogenic memory devices:
  - Orthogonal spin-transfer device:  $\sim 235$  fJ
  - Spin-valve device with Py FL:  $\leq 230$  fJ
  - Three-terminal CSHE device:  $\sim 5.6$  pJ

➔ Surprisingly low write energies due to very low switching currents of 69 (AP→P) and 165  $\mu$ A (P→AP) compared to e.g. 0.9 mA for three-terminal device!

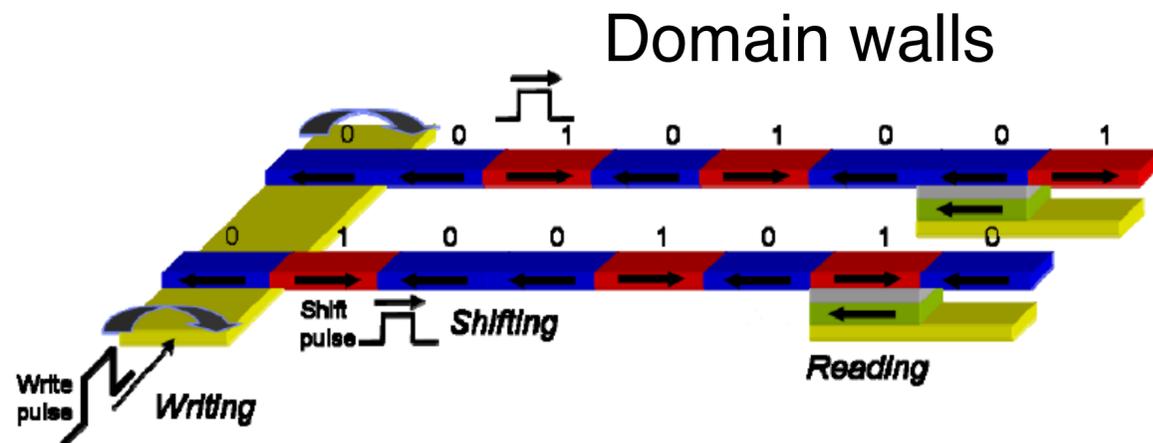
Laura Rehm *et al.*, APL **115**, 182404 (2019)



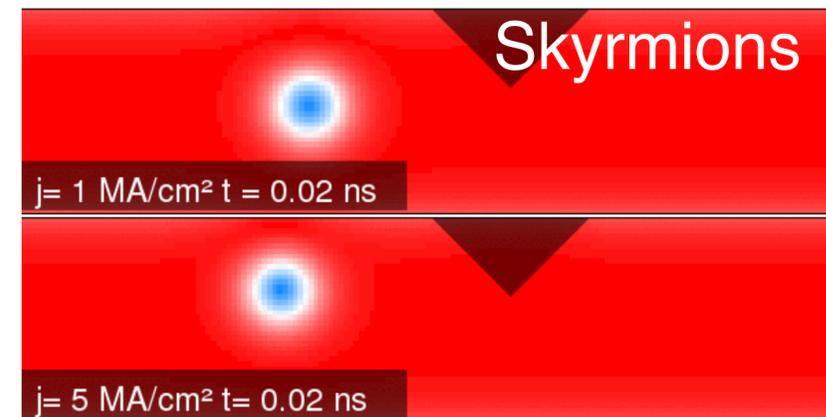
# New Magnetic Technologies



**Idea of moving information without moving the magnetic material!**



S.S.P. Parkin, Racetrack Memory 2008



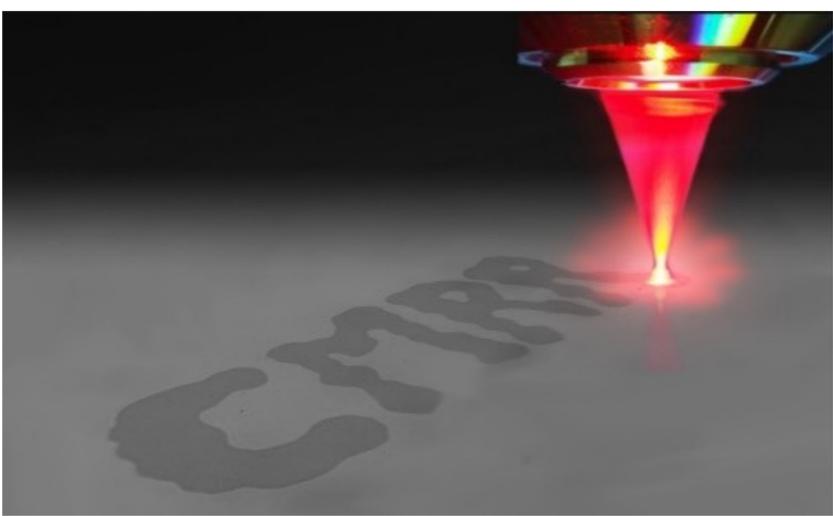
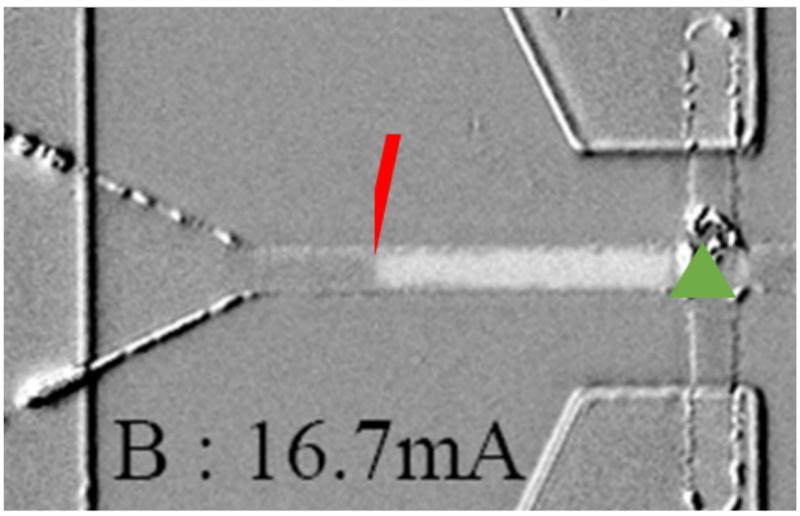
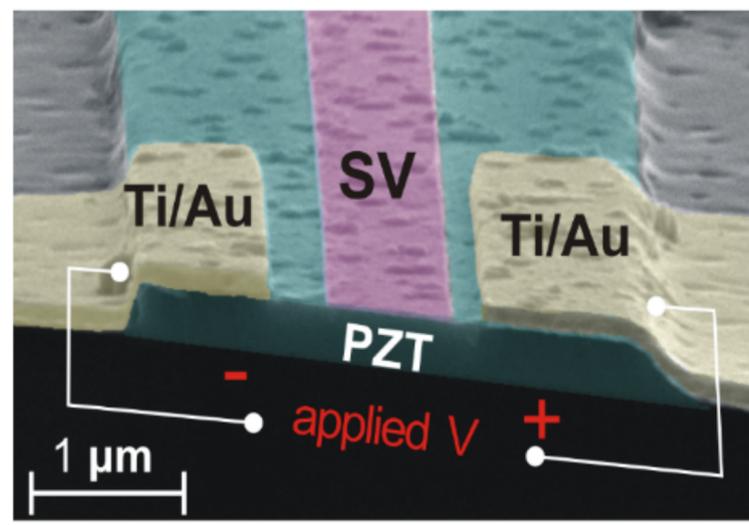
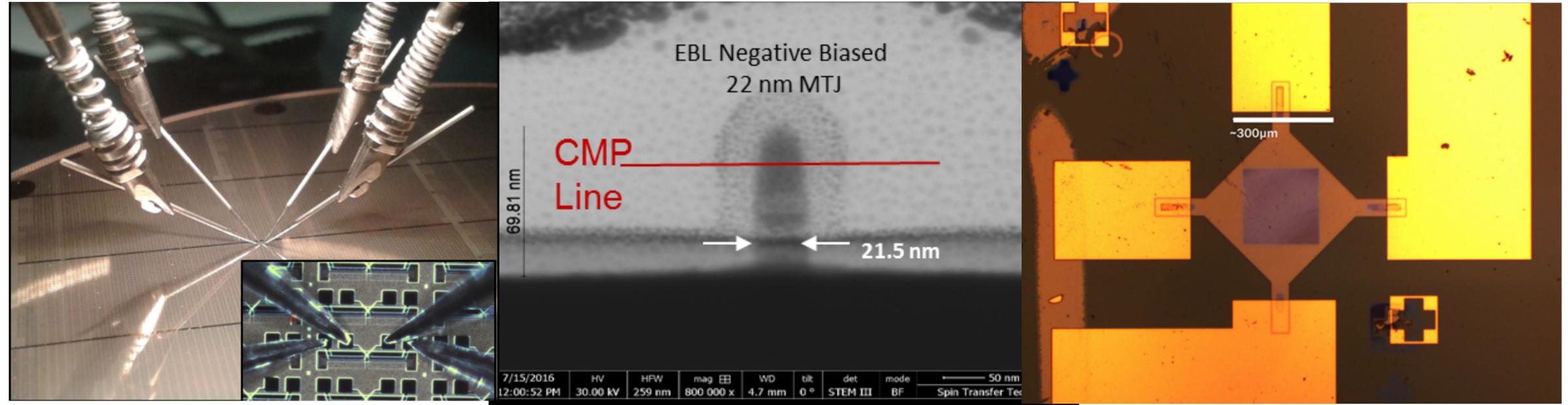
A. Fert, V. Cros, J. Sampaio, *Nature Nano.* **8**, 152 (2013)

J Sampaio *et al.*, *Nature Nano.* **8**, 839 (2013)



# New Magnetic Nanotechnologies

*Nanoelectronics, from new phenomena to low power electronics*



International Associated Laboratory (LIA)





# Summary

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- Magnetic tunnel junction and spin transfer torques
- Applications
- Switching of magnetization, materials and device optimization
- Cryogenic applications



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